Lecture 4:
mmWave Sensing

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香港大學人工智能物联网實驗室

Contents

- Basics of FMCW Radar Signals

- Range Estimation

- Doppler/Velocity Estimation

- Angle Estimation

- Periodicity Estimation

- FMCW Sensing Applications

Why mmWave/RF Sensing?

What information is missing?

Why RF Sensing?

Any other concerns for Vision?

Google Pixel 4

Tesla Vision Update: Replacing Ultrasonic Sensors with Tesla Vision

Safety is at the core of our design and engineering decisions. In 2021, we began our transition to Tesla Vision by removing radar from Model 3 and Model Y, followed by Model S and Model X in 2022. Today, in most regions around the globe, these vehicles now rely on Tesla Vision, our camera-based Autopilot system.

Now it appears radar is back. It's not yet clear which models will get the new radar. The type of radar Tesla intends to market next year is of a frequency that's allocated by the FCC for ADAS use cases, according to Ram Machness, chief business officer at Arbe Robotics, which produces ultra-high-resolution 4D imaging radar.
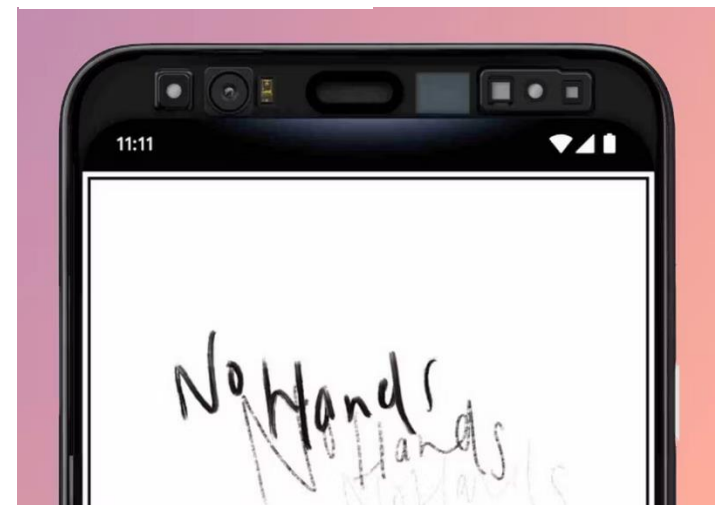
Tesla had originally filed with the FCC to use the new radar — which is described in filings as "76-77 GHz Automotive Radar" — in its vehicles back in June.

"From the frequency of operation (76-77GHz) as well as the mechanical design of the sensor from Tesla's FCC filing, it .... teven Hong, VP and general manager of radar ......ch.

Tesla Adding Radar Back
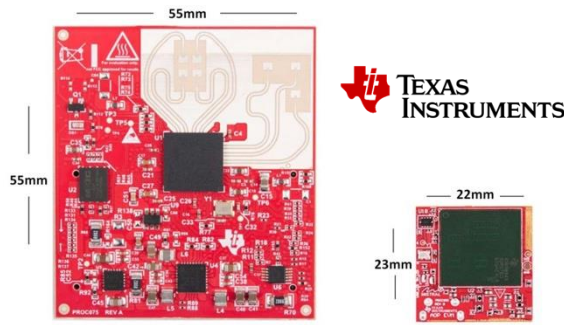
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Contents

- <u>Basics of FMCW Radar Signals</u>
- Range Estimation
- Doppler/Velocity Estimation
- Angle Estimation
- Periodicity Estimation
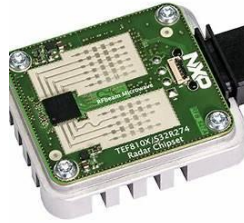- FMCW Sensing Applications

Commodity mmWave Radars

Attribute	Texas Instruments (TI)	Infineon Technologies	NXP Semiconductors	Analog Devices	Vayyar Imaging	Calterah Semiconductor	ICLEGEND
Model	IWR6843 / AWR1843	BGT24MTR12	TEF810X	ADF5904	VTRIG-74	Alps-Pro	ICL1122
Frequency Band	60 GHz / 78 GHz	24 GHz	77 GHz	24 GHz	79 GHz	77-79 GHz	24 GHz
Bandwidth	4 GHz	250 MHz	1 GHz	250 MHz	4 GHz	Up to 5 GHz	250 MHz
Number of Antennas	3 TX, 4 RX	1 TX, 1 RX	3 TX, 4 RX	4 RX	12 TX, 12 RX	4 TX, 4 RX	1 TX, 2 RX

*Price: <US$20 for TI radar; price information is usually not publicly available.

Revisit Chirp Signals

A

t

f

f_{max}

S

B

f_c

T_c

t
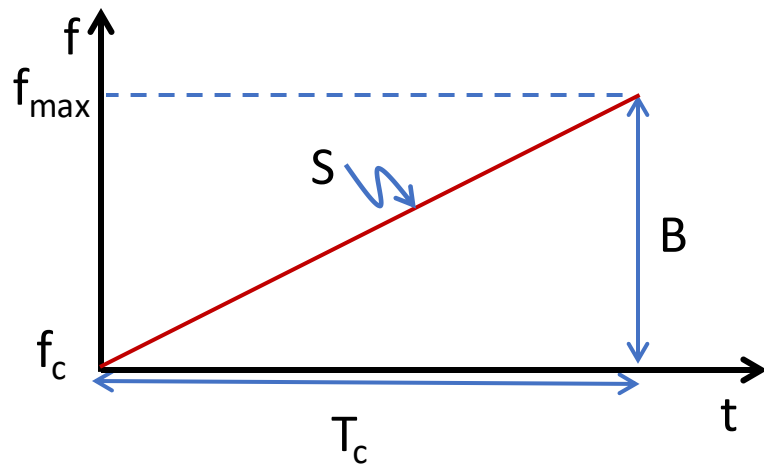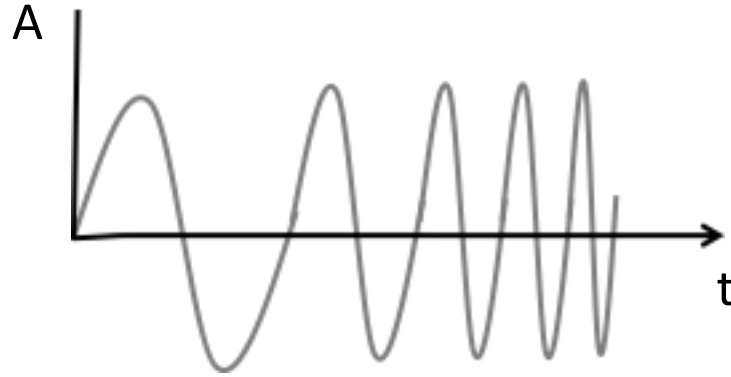
- ## FMCW Radar
  - A Frequency Modulated Continuous Wave radar using chirp signals

- ## Chirp: sinusoid with f increasing linearly with time
  - Amplitude vs. time plot
  - Frequency vs. time plot
    - A slope $S=B/T_c$ defines the rate at which the chirp ramps up
    - f_c: carrier frequency (mmWave frequency band)
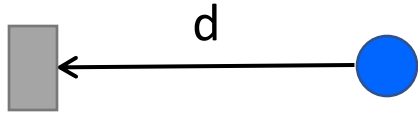
  - Recall CSS in LoRa communication

1Tx-1Rx FMCW Radar

- ## IF (Intermediate Frequency) signal
  - Rx signal and Tx signal are "mixed" together as the IF signal
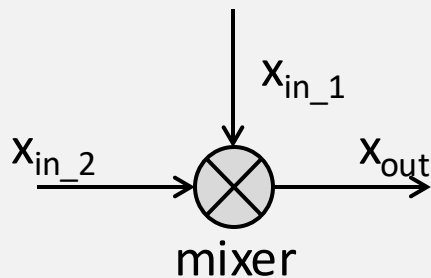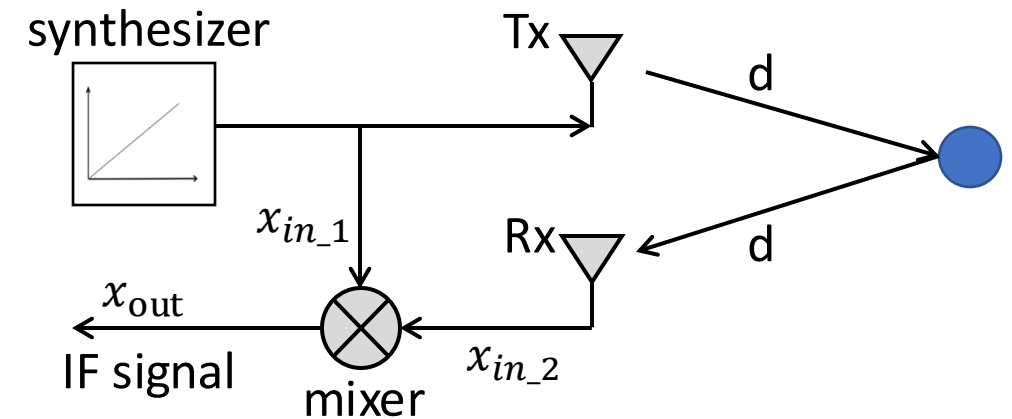
- ## Mixer: 3-port device with 2 inputs & 1 output
  - $x_{in\_1} = \sin(2\pi f_1 t + \phi_1)$
  - $x_{in\_2} = \sin(2\pi f_2 t + \phi_2)$
  - $x_{out} = \sin[2\pi(f_1 - f_2)t + (\phi_1 - \phi_2)]$
  - Eliminate the carrier frequency f_c

FMCW Radar Sensing

How to estimate the range of an object?

What if there are multiple objects?

How close can two objects be while still being separatable?

How to measure the velocity of the objects?

How to find the direction of the objects?

Can we also monitor periodic motions such as vibrations, heartbeats?
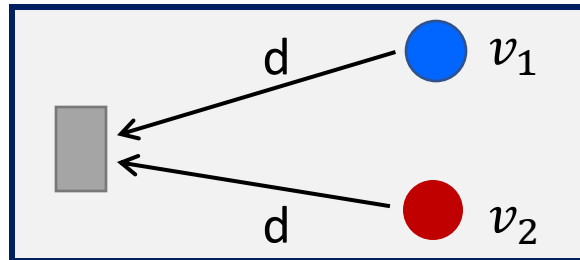
- Range
- Doppler
- Angle (Angle of Arrival, AoA)

Contents

- Basics of FMCW Radar Signals
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- Angle Estimation
- Periodicity Estimation
- FMCW Sensing Applications

IF Signal – Single Object
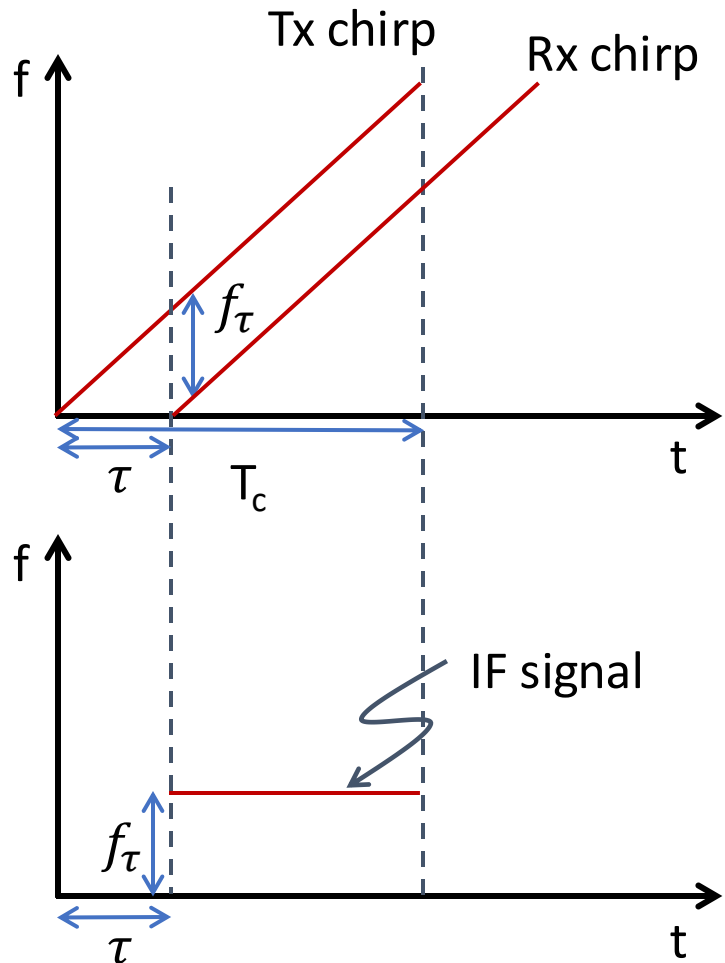
- Rx signal is a delayed version of the Tx signal, with delay τ.

- A single object in front of the radar produces an IF signal with a constant frequency of $f_\tau = S\tau$

$$\tau = \frac{2d}{c}: \underline{\text{round-trip time}} \text{ (RTT) between the radar and the object}$$

$$f_\tau = S\tau = \frac{2dS}{c} \rightarrow d = \frac{cf_\tau}{2S}$$

- τ (and thus the non-overlapping part of Tx and Rx signals) is typically very small and negligible compared to T_c.
- E.g., for a max d of 100m and $T_c = 40us$, $\frac{\tau}{T_c} = \frac{1}{60} = 1.7\%$.

Multiple objects

Tx chirp
Rx chirps

f

t

f

IF signal

t
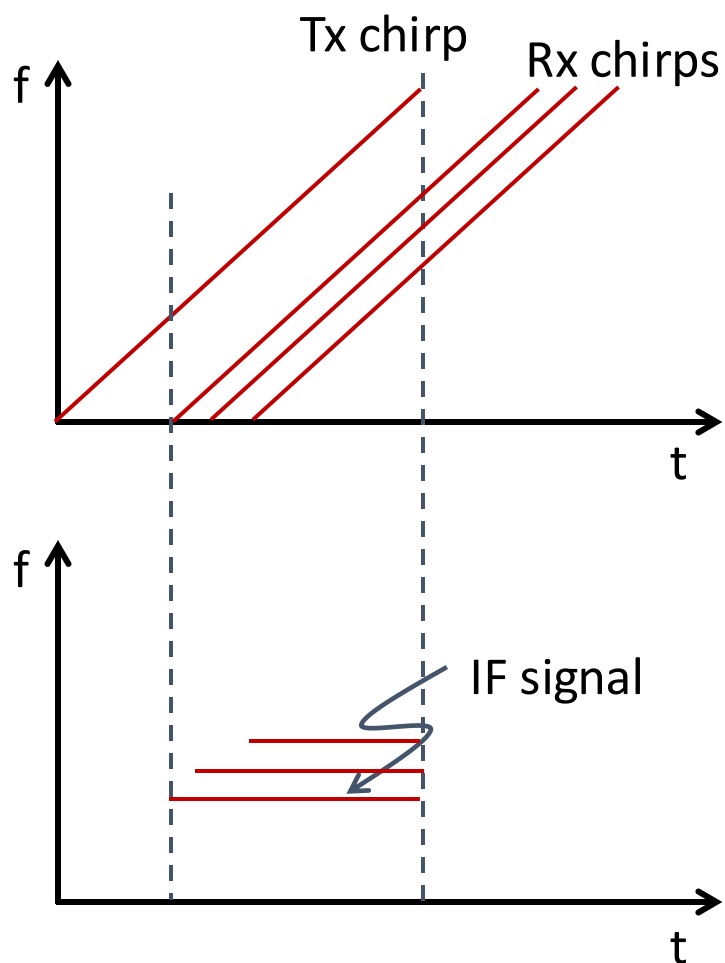
- Multiple objects → multiple reflected copies of chirps

A frequency spectrum of the IF signal will reveal multiple tones, the frequency of each being proportional to the range of each object from the radar

f_τ → d

Range-FFT

IF frequency spectrum

f
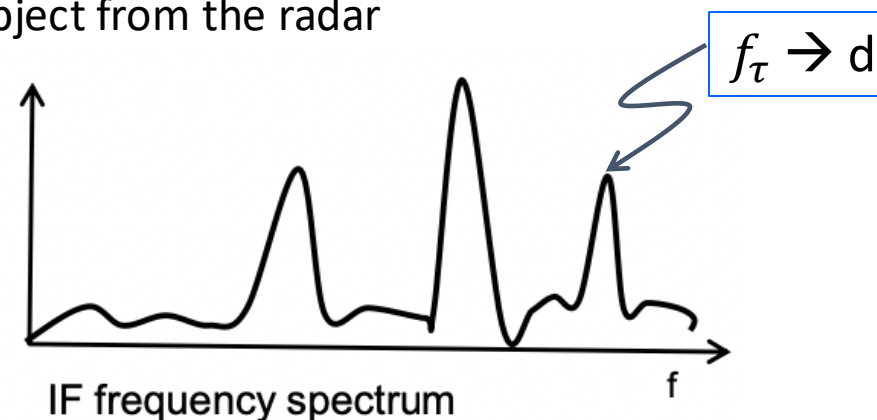
- If two objects are very close to each other, can they be separated?
- What's the minimum separation of two objects that can be resolved?

Range Resolution

- The ability to resolve/separate two closely spaced (in range dimension) objects

Tx chirp

Rx chirps

IF frequency spectrum
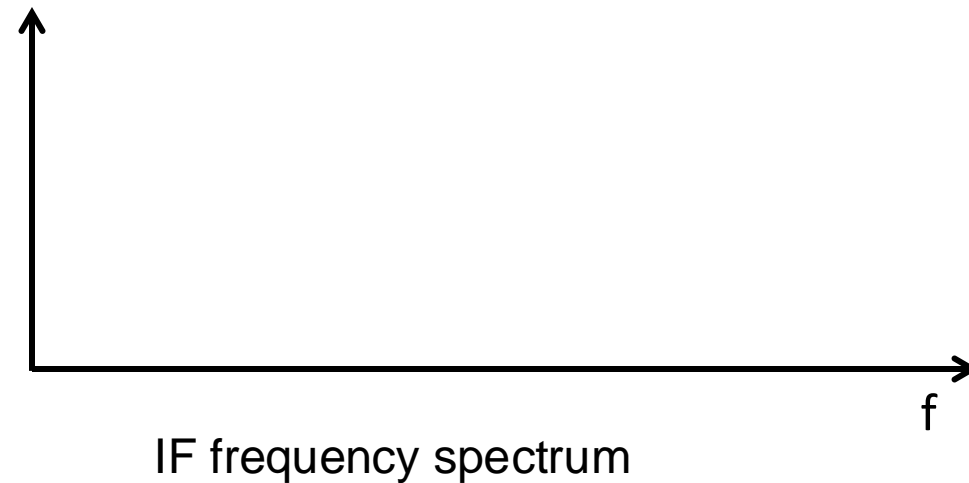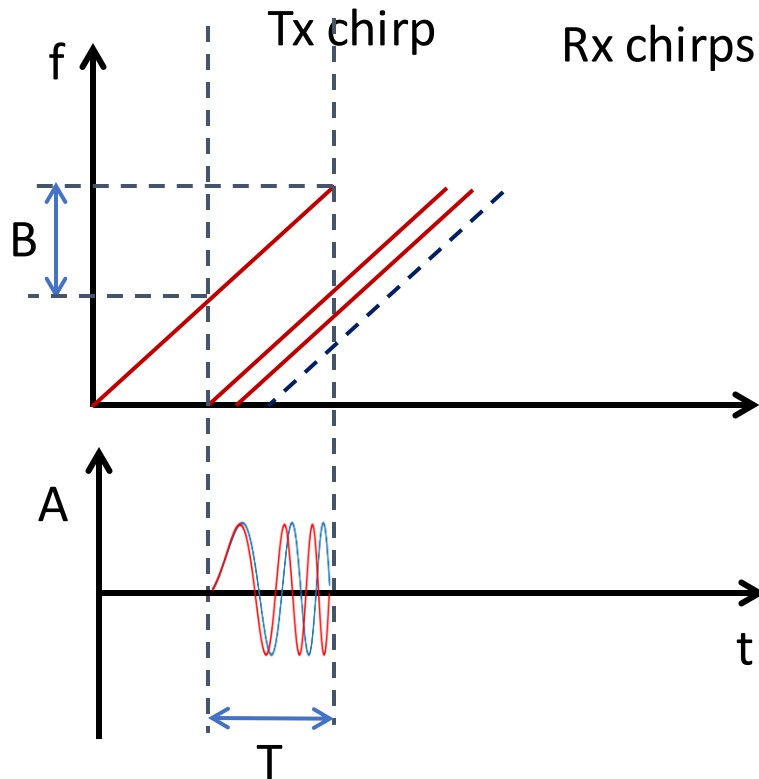
Fourier Transforms

One single frequency
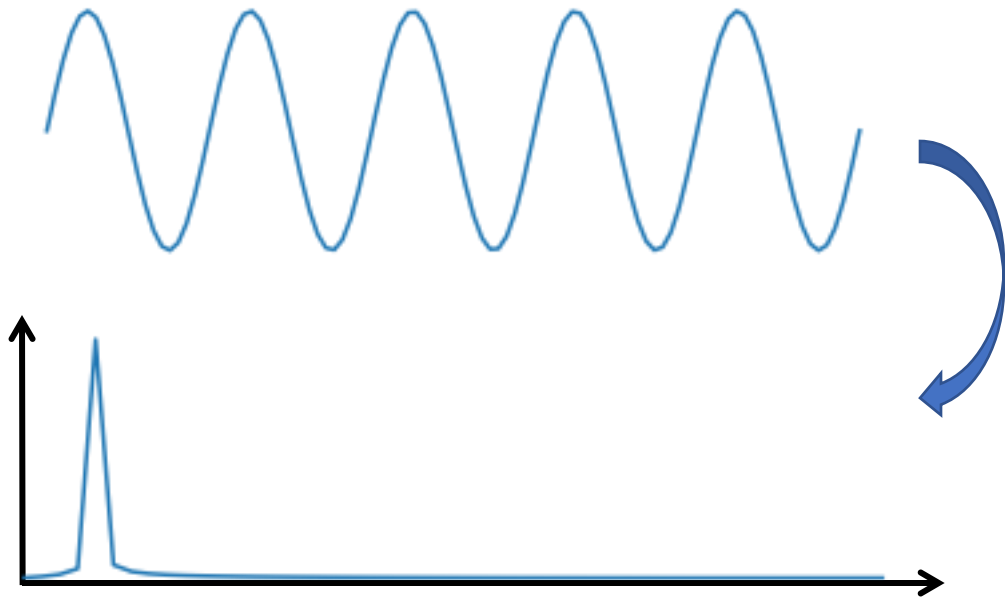
Two sufficiently different frequencies

FFT

A visual intro to FFT: https://www.youtube.com/watch?v=spUNpyF58BY
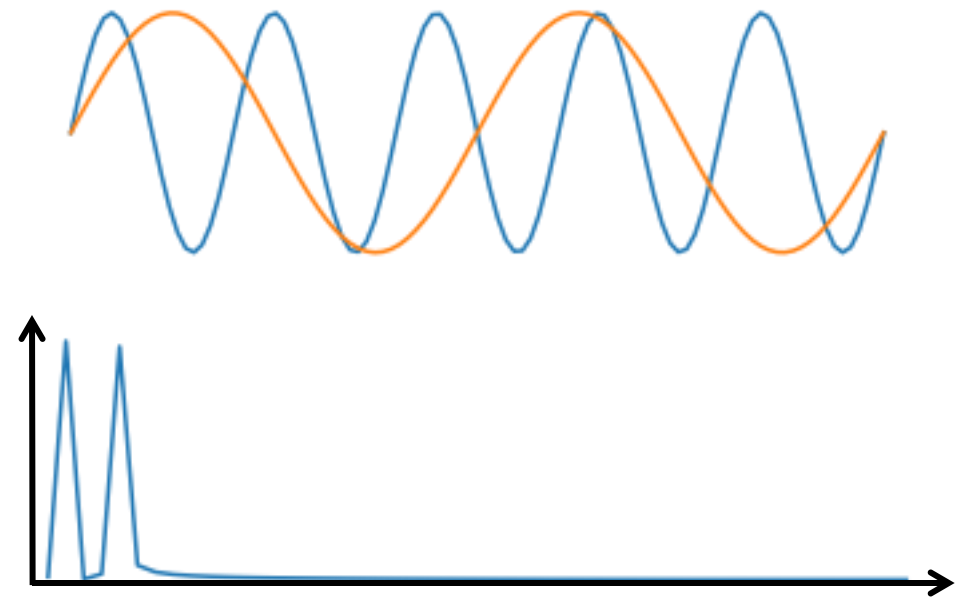
Fourier Transforms

Two close frequencies
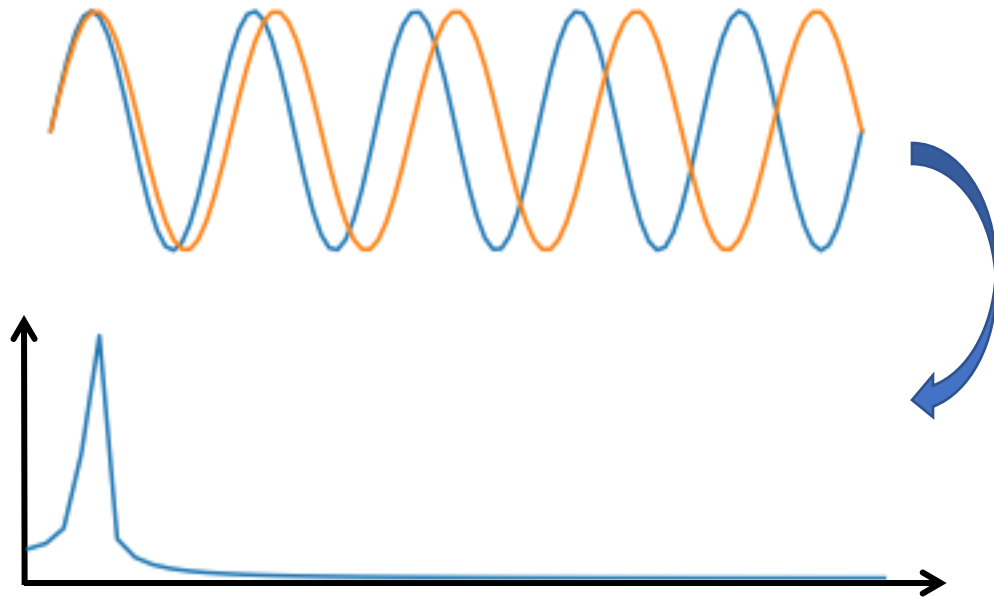
Two close frequencies with a longer observation window

FFT
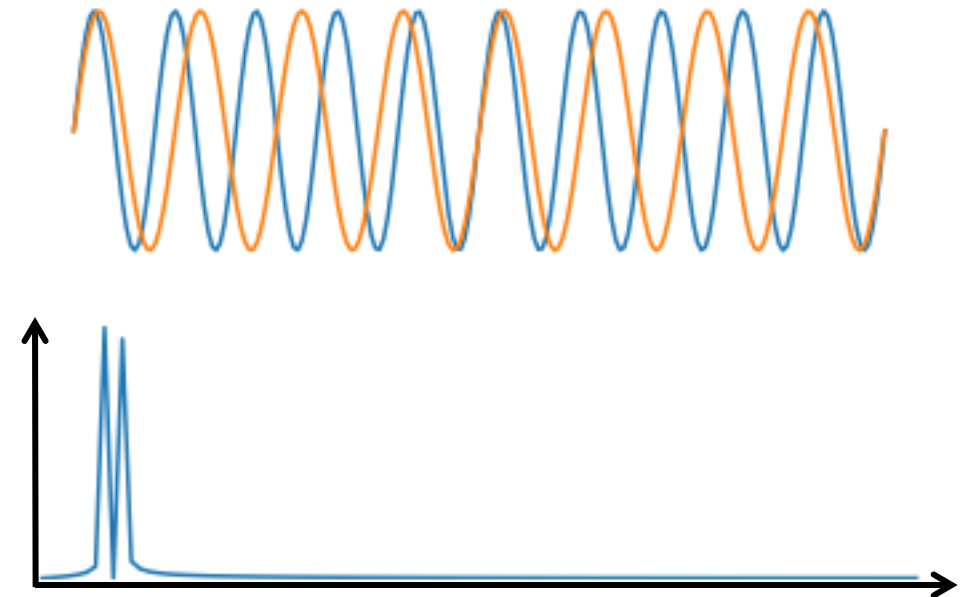
Longer observation period → higher frequency resolution.
In general, frequency resolution = 1/T for an observation window of T.

Range resolution vs. Bandwidth

- Range resolution improves with increased observation period T, i.e., the length of the IF signal
- Proportionally increases the bandwidth
- Thus: Larger bandwidth → Better resolution

Tx chirp

Rx chirps

f

$2B$

A

t

$2T$

IF frequency spectrum
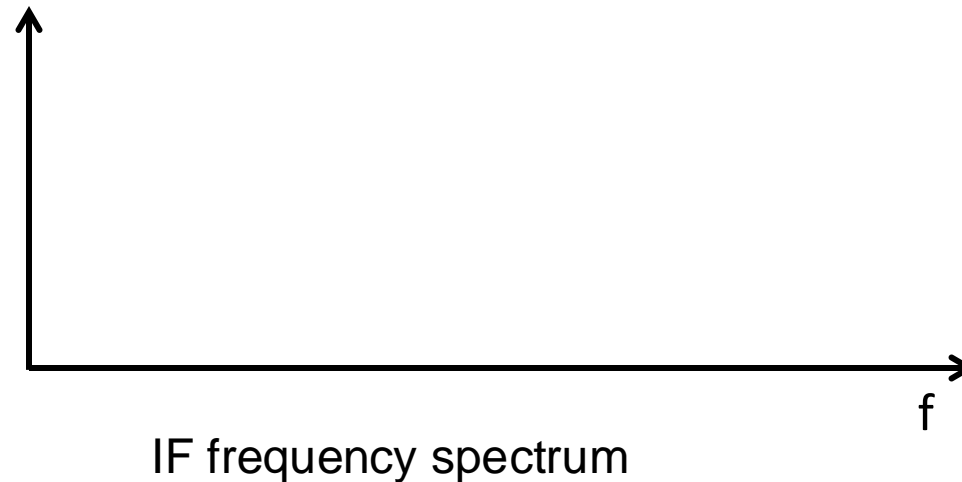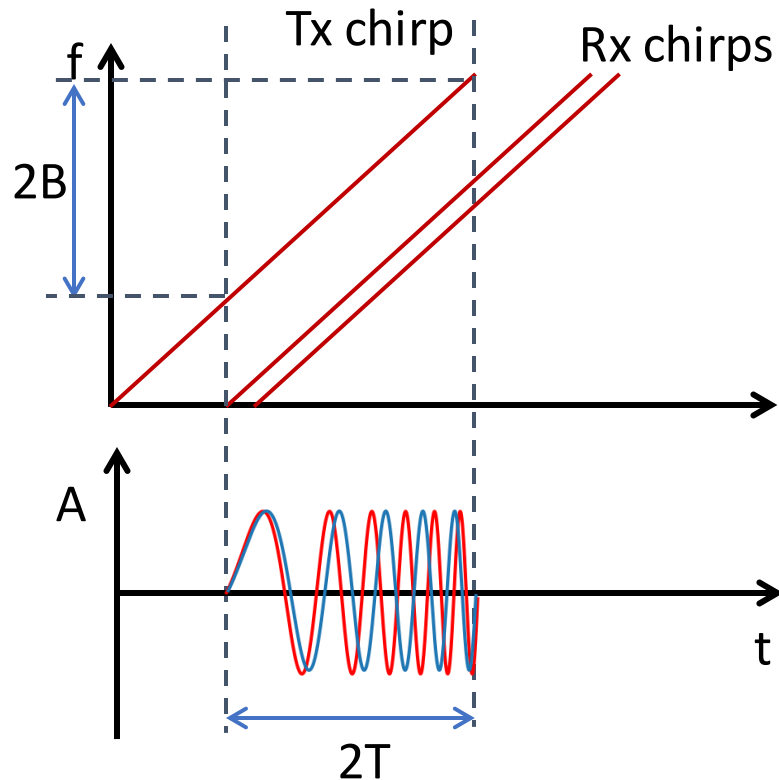
Range resolution vs. Bandwidth

- ## Recall
  - An object at a distance d results in an IF tone of frequency $f_\tau = S2d/c$
  - Two tones can be resolved in frequency if $\Delta f > \frac{1}{T}$

- ## Range resolution of a radar?

Two objects at d_1 and d_2 with a distance difference Δd, their IF frequency difference is $\Delta f = \frac{S2\Delta d}{c}$. The observation period is T_c, and thus $B = ST_c$.

To resolve the two frequencies/objects, we need to have

$$\Delta f > \frac{1}{T_c} \Rightarrow ?$$

The Range Resolution depends on only the bandwidth:

$$d_{res} = \frac{c}{2B}$$

Range resolution vs. Bandwidth

- Typical values for Bandwidth and Range resolution

Bandwidth	Range Resolution	
4GHz	3.75 cm	TI FMCW Radar 3.56 GHz
1GHz	15 cm	
600 MHz	25 cm	
160 MHz	0.9375 m	WiFi 802.11ax / WiFi 6
80 MHz	1.875 m	WiFi 5GHz
40 MHz	3.75 m	WiFi 5GHz
20 MHz	7.5 m	WiFi 2.4GHz

The Range Resolution depends on only the bandwidth:

$$d_{res} = \frac{c}{2B}$$

1. What is the range resolution between separated Tx and Rx?
2. What about non-RF signals, e.g., acoustic signals?

Ranging summary

- IF signal consists of one or multiple tones.
- The frequency (f) of each tone is proportional to the distance (d) of the corresponding object

$$f_\tau = S2d/c$$

- Range resolution:

$$d_{res} = c/2B$$

- Range-FFT can be performed on the IF signal to estimate range.
  - Measure the Frequency, not the Time!

synthesizer

Tx

d

Rx

d

IF signal

mixer

$f_\tau \rightarrow$ d

Range
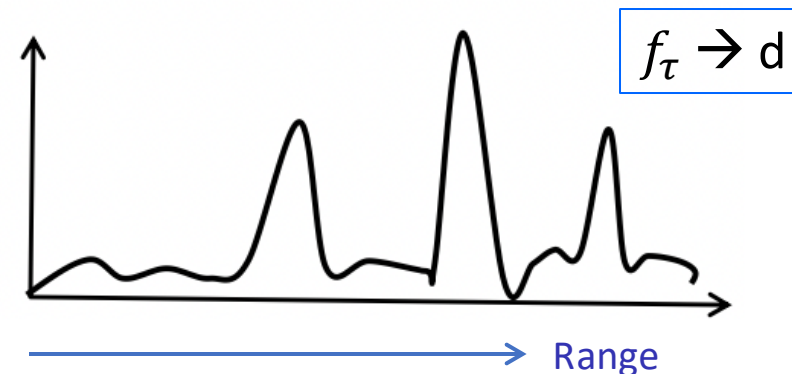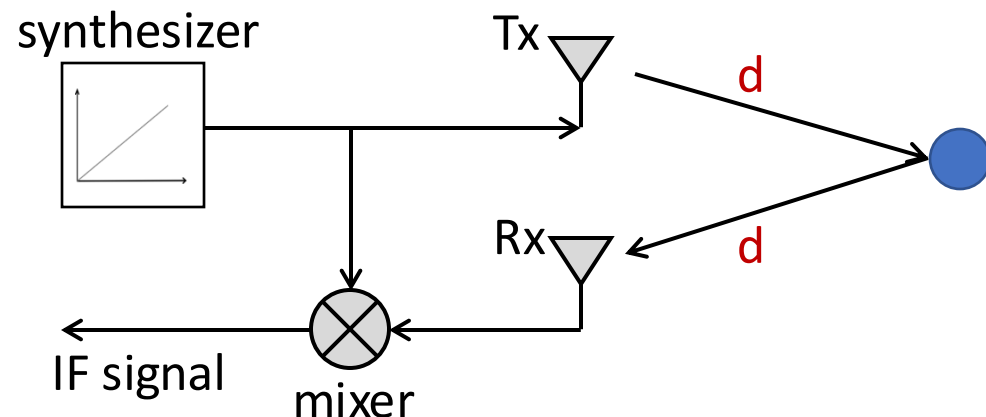
Channel Impulse Response
Power Delay Profile (Amplitude only)

Quiz

Quiz Time
Let's have
some fun!

- Given the FMCW radar signal in the diagram
- (1) Assume it works on the 60GHz frequency band, what is the wavelength of the radar signal?

- (2) What is the range resolution of this radar?

- (3) Suppose we observe a frequency of 1MHz in the IF signal, what is the object's range?

$S = 50\text{MHz}/\mu s$

$T_c = 40\mu s$

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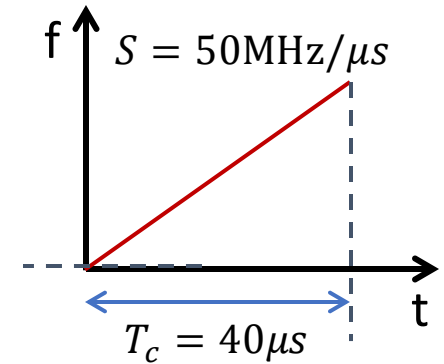
Ranging summary

- Two objects equidistant from the radar. How will the range–FFT look like?
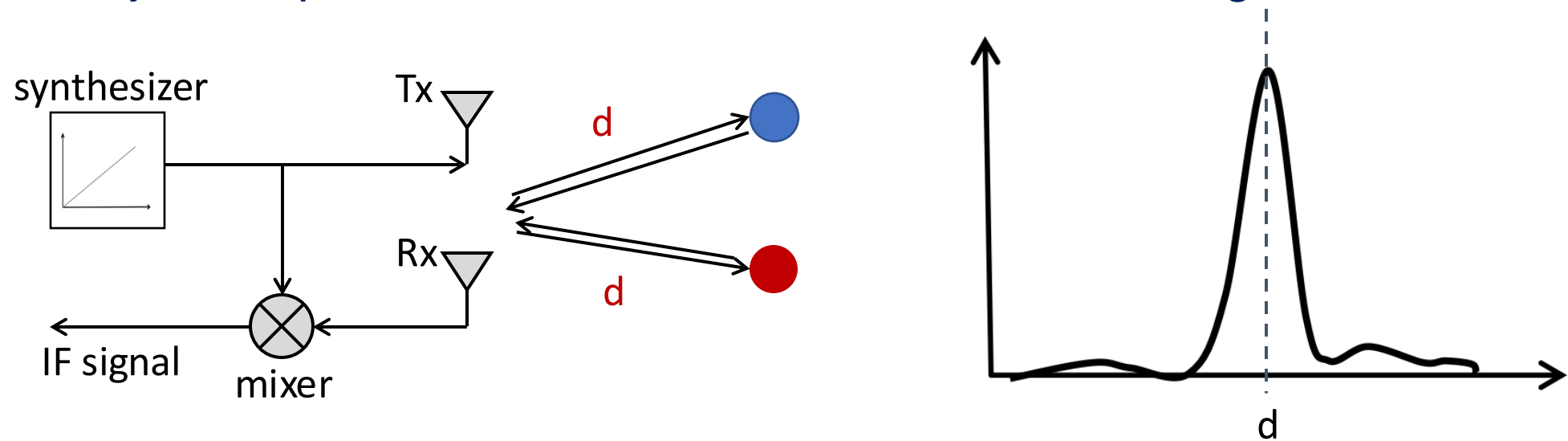
- How do we separate these two objects?
  - Doppler-FFT

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- Basics of FMCW Radar Signals

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- <u>Doppler/Velocity Estimation</u>

- Angle Estimation

- Periodicity Estimation

- FMCW Sensing Applications

Doppler Effect

- The change in frequency of a wave in relation to an observer who is moving relative to the wave source

The Phase of IF signal

Tx chirp

A

t

Rx chirp

A

t

τ

IF signal

A

t
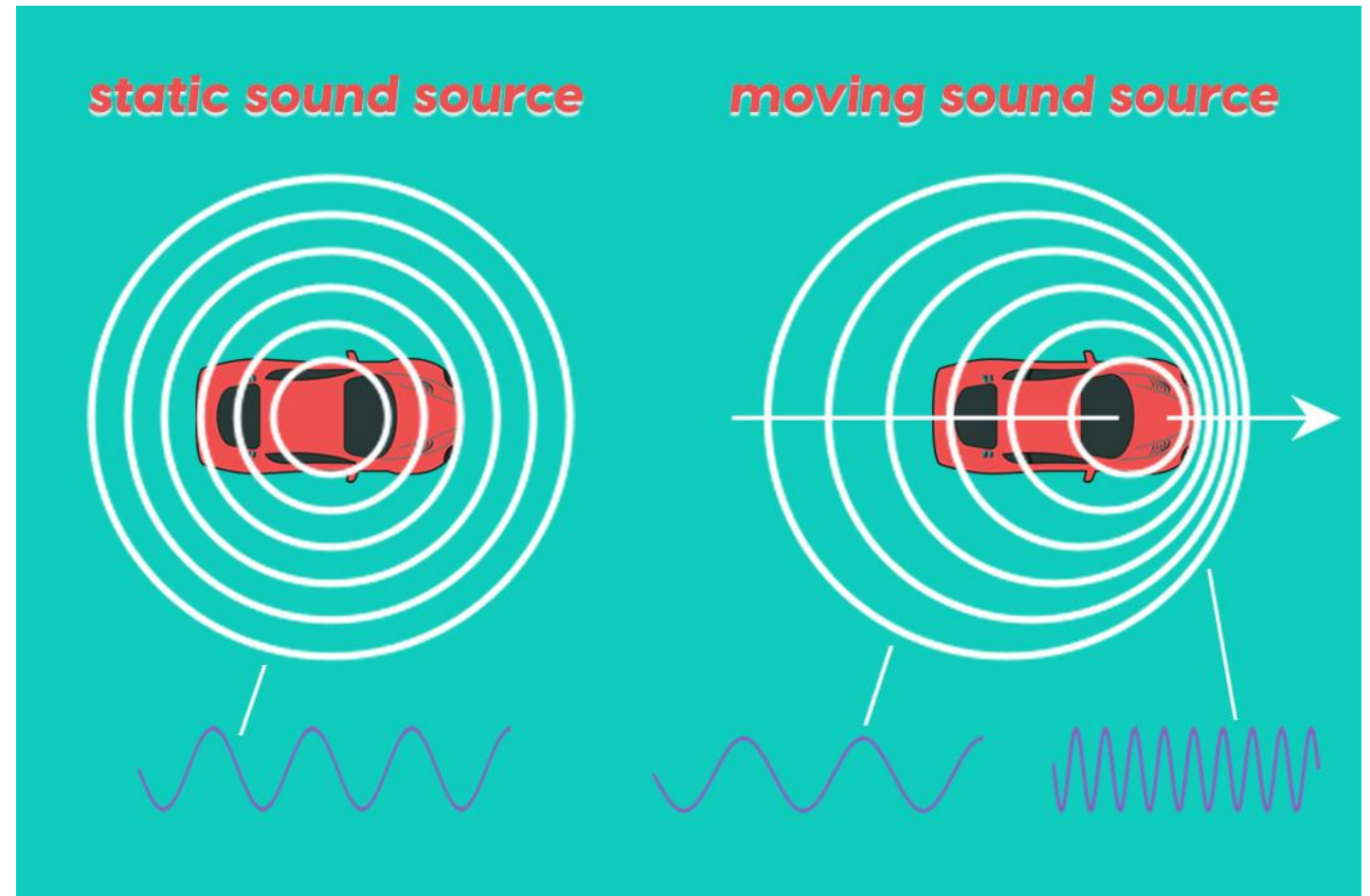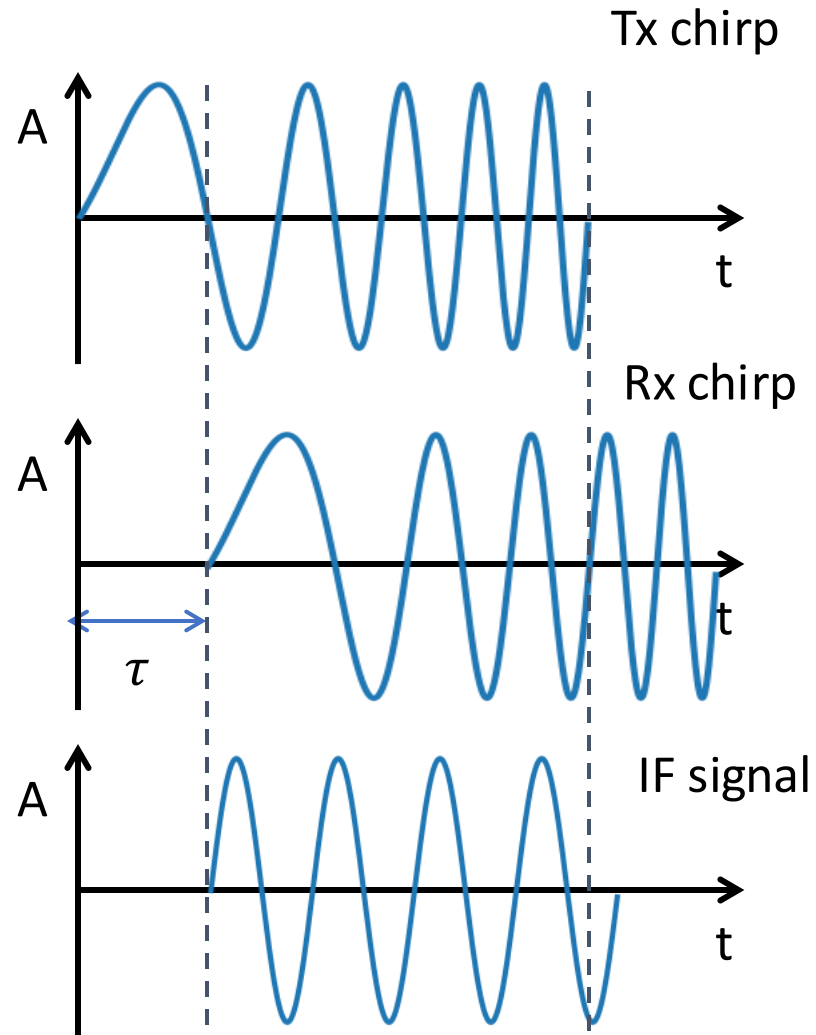
- Assume one object at a distance d_0, the resulted IF signal:

$$Asin(2\pi f_0 t + \phi_0)$$

- Frequency: $f_0 = \dfrac{S2d_0}{c}$

- Phase $\phi_0 = -2\pi f \dfrac{2d_0}{c} = -4\pi \dfrac{d_0}{\lambda}$: the difference of the initial phases of the Tx and Rx chirps (Rx chirp delayed by ϕ_0)

The Phase of IF signal

Tx chirp
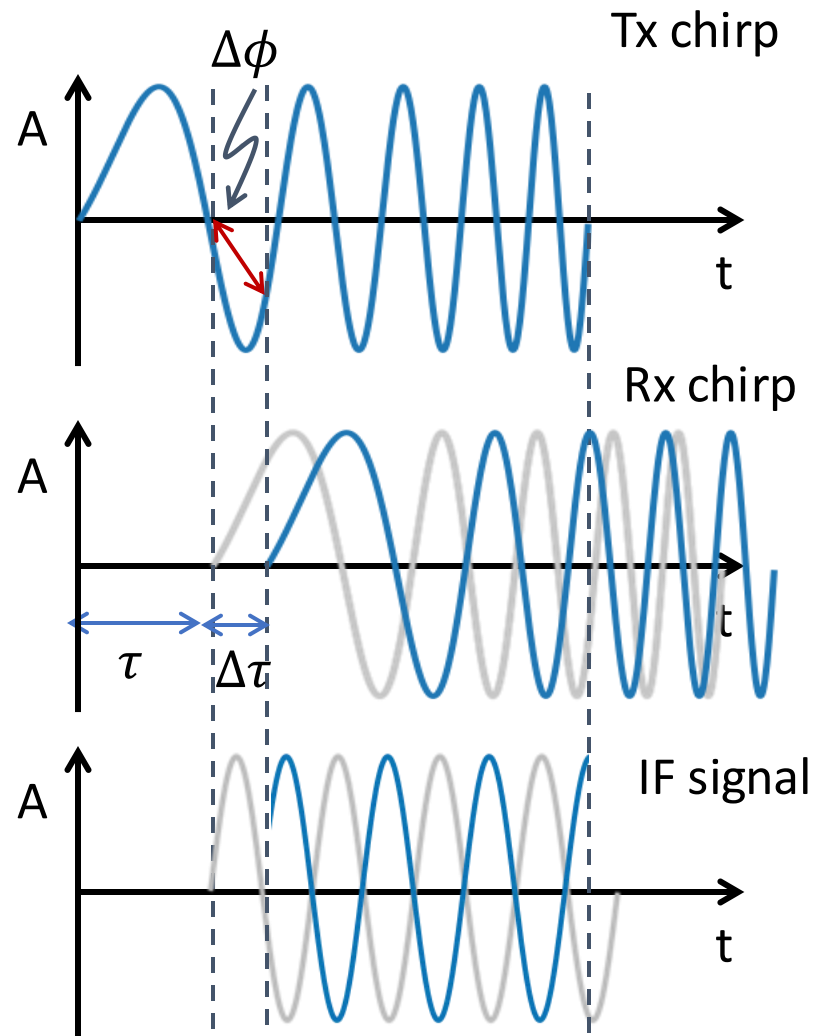
Rx chirp

IF signal

- What happens if the RTT delay changes a bit by $\Delta\tau$ (the object moves for a short distance Δd)? The phase of Rx chirps changed by

$$\Delta\phi = 2\pi f_c \Delta\tau = \frac{4\pi\Delta d}{\lambda}$$

- The IF signal experiences the same amount of phase changes

$$A\sin(2\pi ft + \phi_0 + \Delta\phi)$$

Equal to the <u>phase</u> of the peak in FFT response

Phase changes: An example

- Assuming a center frequency of 77GHz ($\lambda \approx 4$ mm), what is the phase change if an object moves by 1mm ($\approx \lambda/4$)?
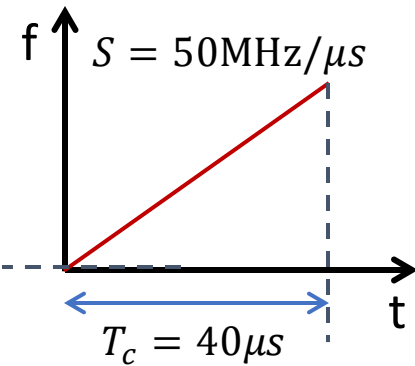
$$\Delta\phi = \frac{4\pi\Delta d}{\lambda} = \pi$$

Huge!

- The frequency of the IF signal changes by

$$\Delta f = \frac{S2\Delta d}{c} = 333\text{ Hz}$$

Small!

$S = 50\text{MHz}/\mu s$

$T_c = 40\mu s$

The phase of the IF signal is extremely sensitive to distance/range changes of an object.

Phase changes due to small motion
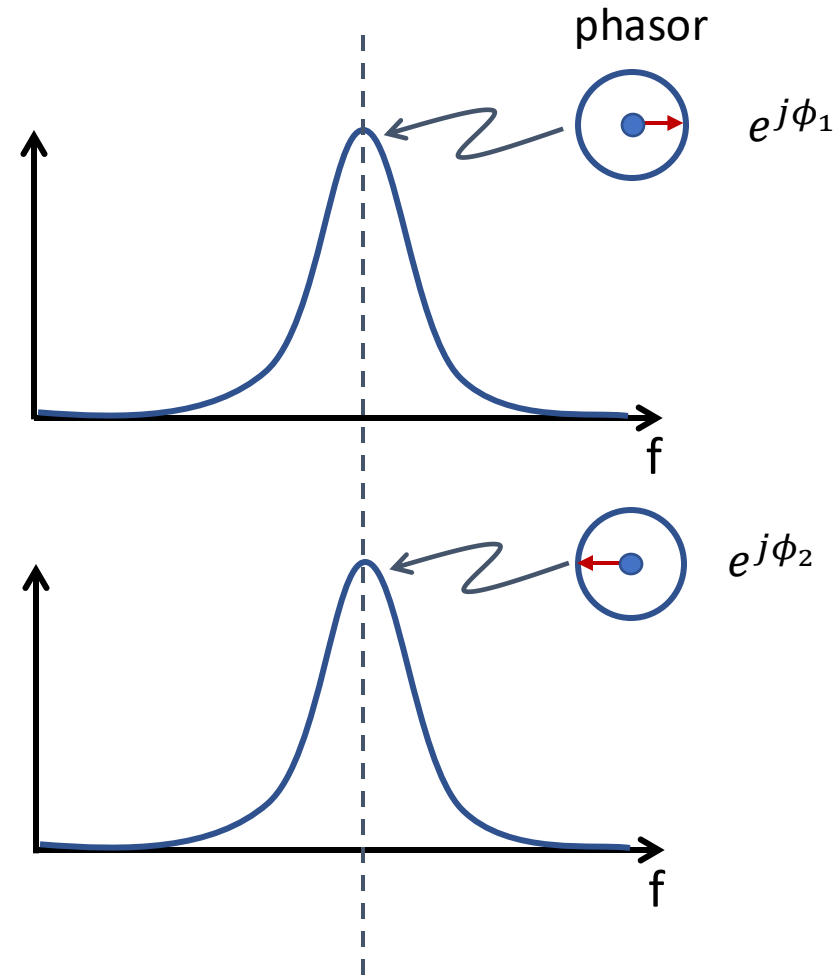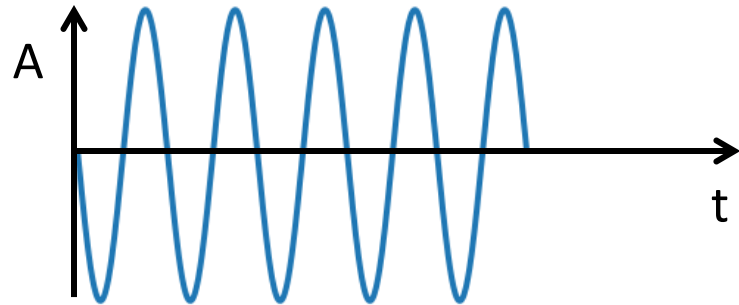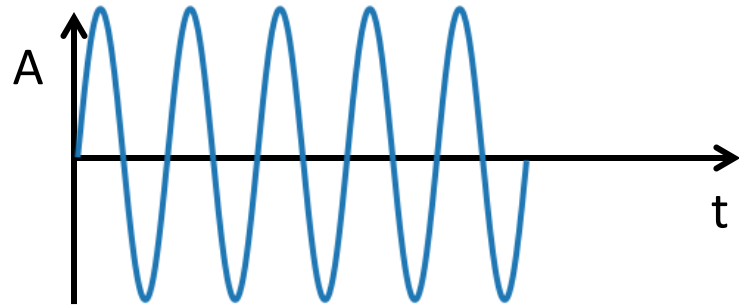
Measure velocity from phase changes
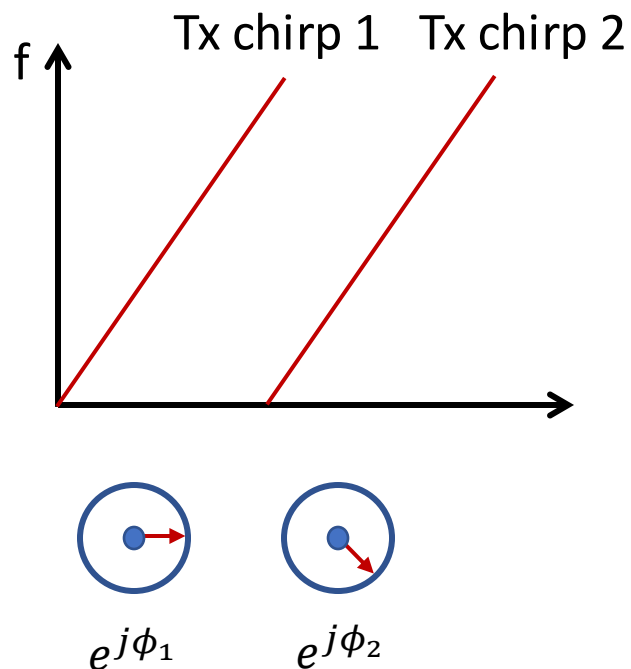
- Transmit continuous chirps separated by T_c
- Consider <u>one</u> moving object
- Range-FFT for <u>each chirp</u> produces the same peak, but with <u>different phase</u>
- The phase difference $\Delta\phi$ implies the moving speed

$$\Delta\phi = \frac{4\pi\Delta d}{\lambda} = \frac{4\pi v T_c}{\lambda}$$

$$v = \frac{\lambda\Delta\phi}{4\pi T_c}$$

Doppler-FFT

$e^{jk\omega_1}, \omega_1 = 4\pi v T_c/\lambda$

$$\phi_1[0] = \frac{4\pi v T_c}{\lambda} \cdot 1$$

$$\phi_1[1] = \frac{4\pi v T_c}{\lambda} \cdot 2$$

$$\phi_1[2] = \frac{4\pi v T_c}{\lambda} \cdot 3$$

...
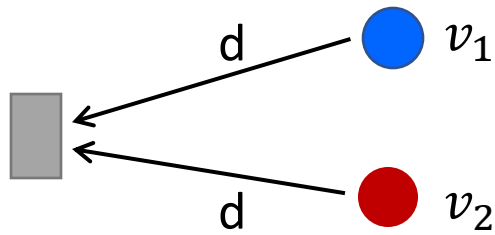
$$\phi_1[N-1] = \frac{4\pi v T_c}{\lambda} \cdot N$$

- <u>Doppler-FFT</u>: FFT on the sequence of phasors corresponding to the range-FFT peaks
- Resolve two objects at the same *d* but moving at different speeds

d v_1

d v_2

f

Tx chirps

t

$A_1 e^{jk\omega_1} + A_2 e^{jk\omega_2}$

Doppler-FFT

$e^{jk\omega_2}$ $e^{jk\omega_1}$

f
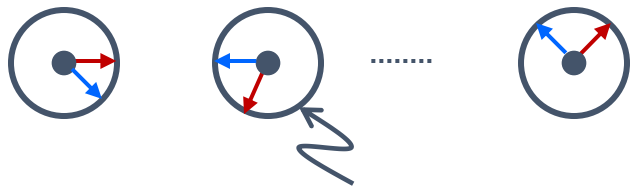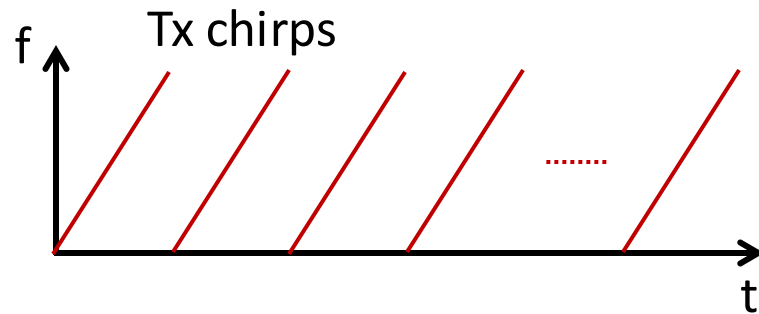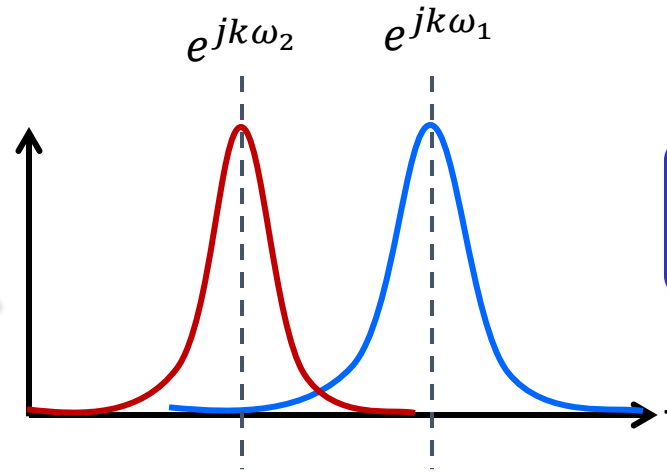
$$v_1 = \frac{\lambda \omega_1}{4\pi T_c}, v_2 = \frac{\lambda \omega_2}{4\pi T_c}$$
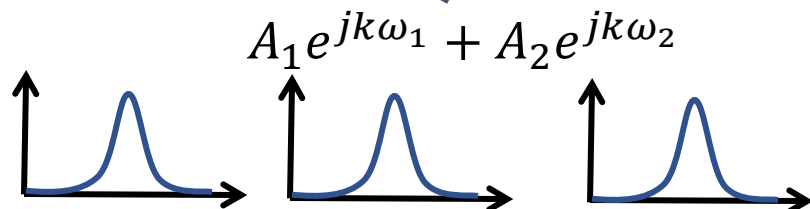
Can we still directly calculate phase differences of the IF signal to calculate the speeds? 🤔

Velocity resolution

- **Velocity resolution of Doppler-FFT?**
  - Minimum separation between v_1 and v_2 so that they show up as two distinguishable peaks in Doppler-FFT

$$\Delta \omega = \frac{4\pi \Delta v T_c}{\lambda} > \frac{2\pi}{N}$$
$$\rightarrow \Delta v > \frac{\lambda}{2NT_c}$$

$$v_{res} = \frac{\lambda}{2T_f}$$
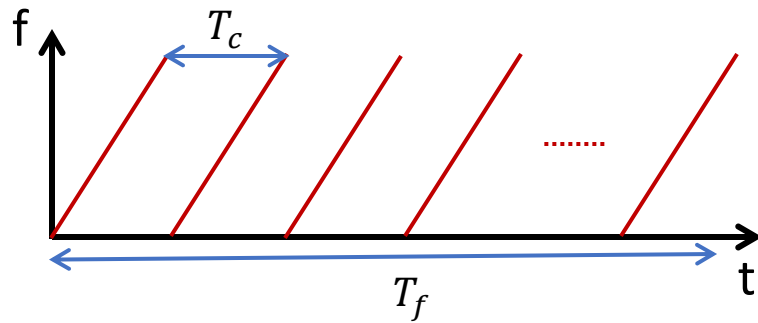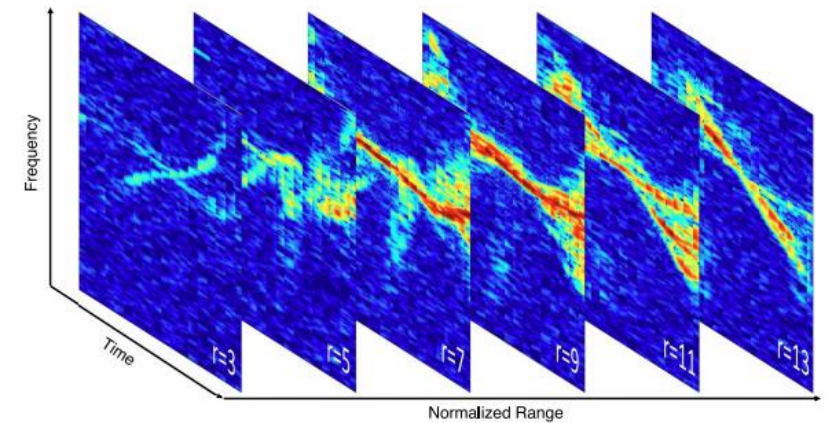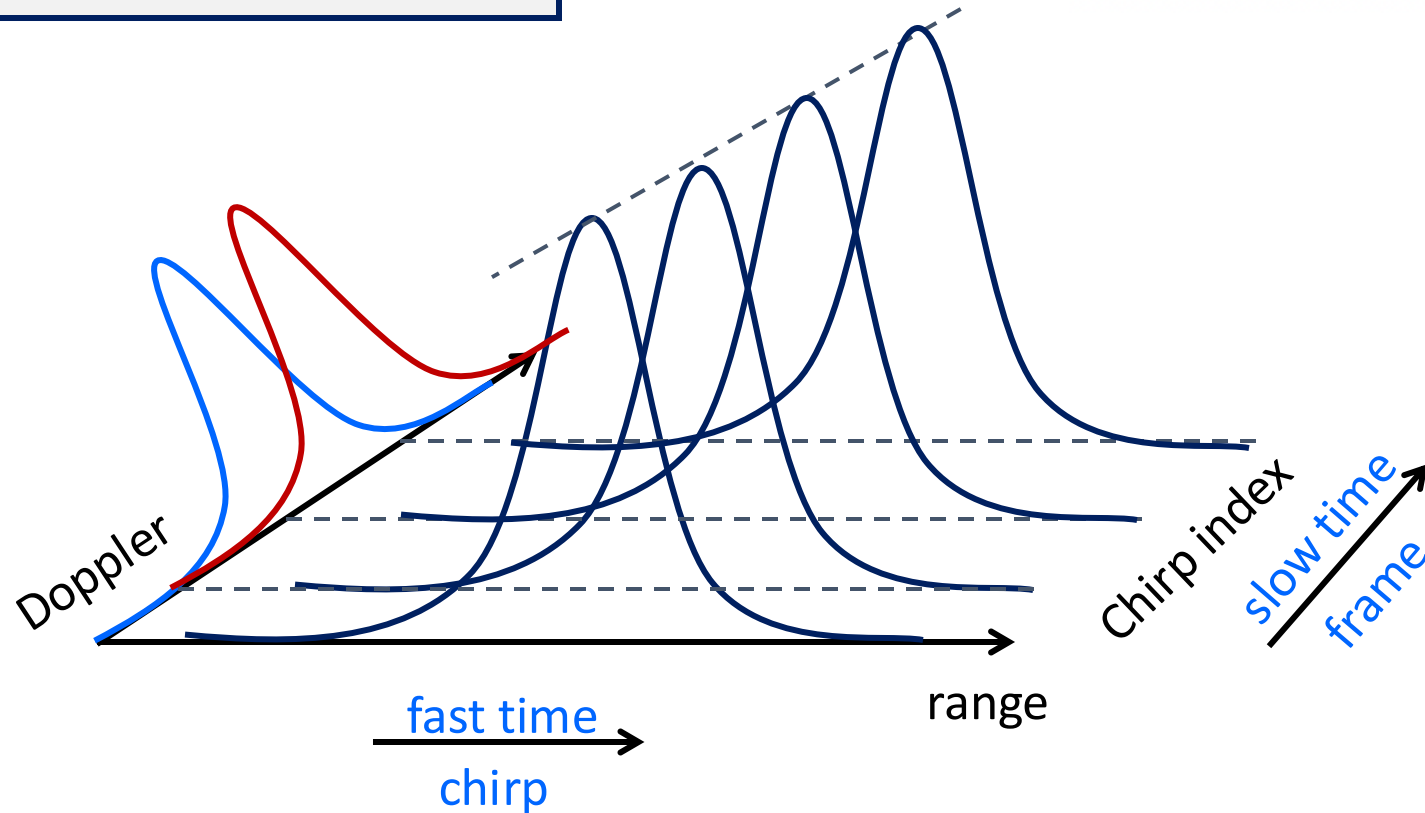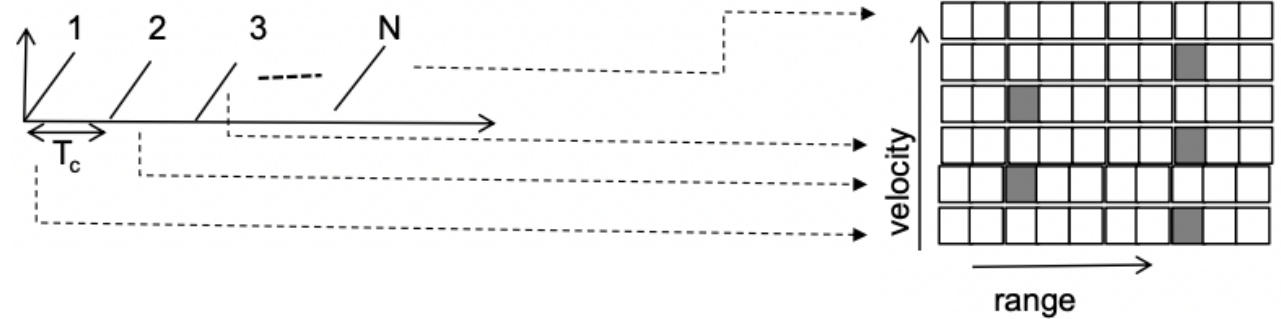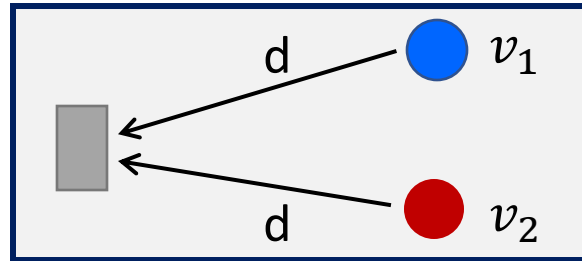
- FFT Resolution: FFT on N discrete observations can separate two radian frequencies ω_1 and ω_2 if $|\omega_1 - \omega_2| > 2\pi/N$
- T_c: Chirp duration
- T_f: Frame duration (N consecutive chirps)

Range-Doppler 2D-FFT

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- Basics of FMCW Radar Signals
- Range Estimation
- Doppler/Velocity Estimation
- <u>Angle Estimation</u>
- Periodicity Estimation
- FMCW Sensing Applications

Angle Estimation

- What if $v_1 = v_2$?
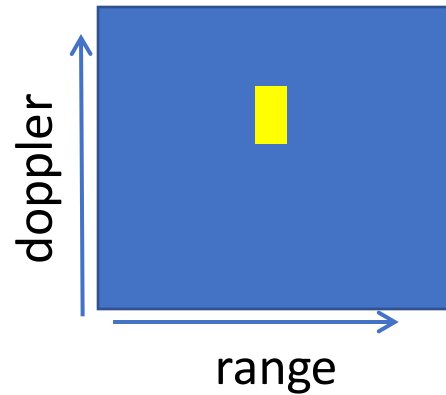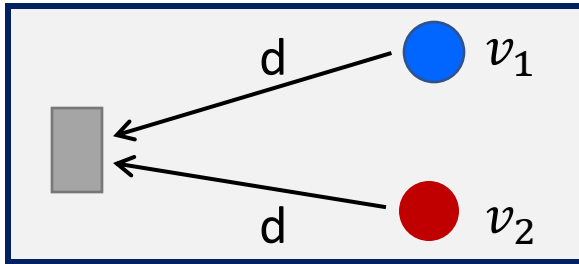
Single peak in the range-Doppler 2D-FFT plot, as they have the same range and velocity.

How do we separate the two objects?

Angle of Arrival (AoA)

- How to estimate the angle of arrival of an object?

- How to estimate AoAs of multiple objects at different angles?

- Angle resolution?

- What is the Field of View (FoV)?

AoA Estimation

- Recall: A small change Δd in **d** results in a phase change $\Delta\phi$
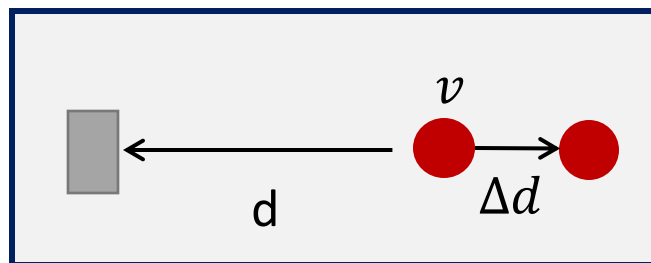
$$\Delta\phi = 4\pi\Delta d/\lambda$$

- AoA estimation requires multiple antennas
  - The slight difference in propagation distances from the object to each antennas also lead to phase changes in the 2D-FFT.

$$\Delta\phi = 2\pi\Delta d/\lambda$$

Why 2π?

AoA Estimation

Tx   Rx

doppler / range
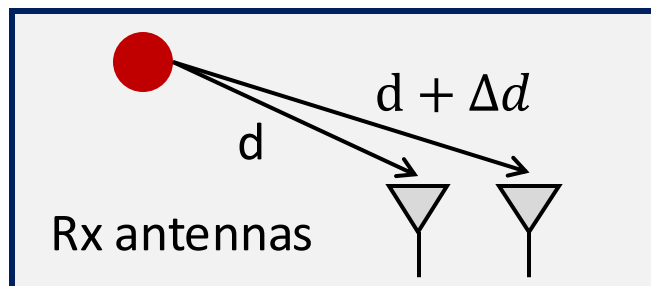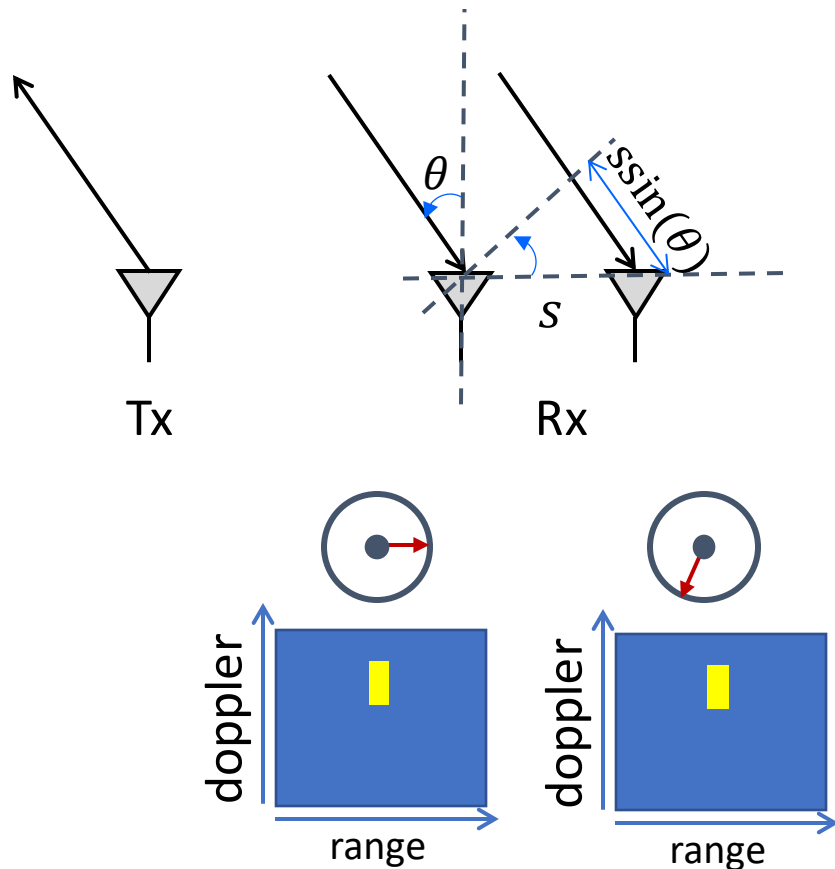
- The measured phase difference can be used to infer AoA

$$\Delta\phi = \frac{2\pi s \sin(\theta)}{\lambda}$$

$$\rightarrow \theta = \sin^{-1}\left(\frac{\lambda\Delta\phi}{2\pi s}\right)$$

AoA Estimation
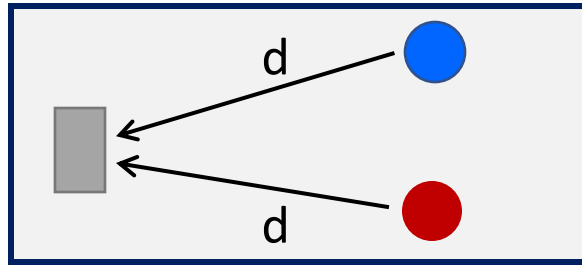
- The method will not work in presence of multiple objects
  - Multiple phase components

- An array of more receive antennas is needed
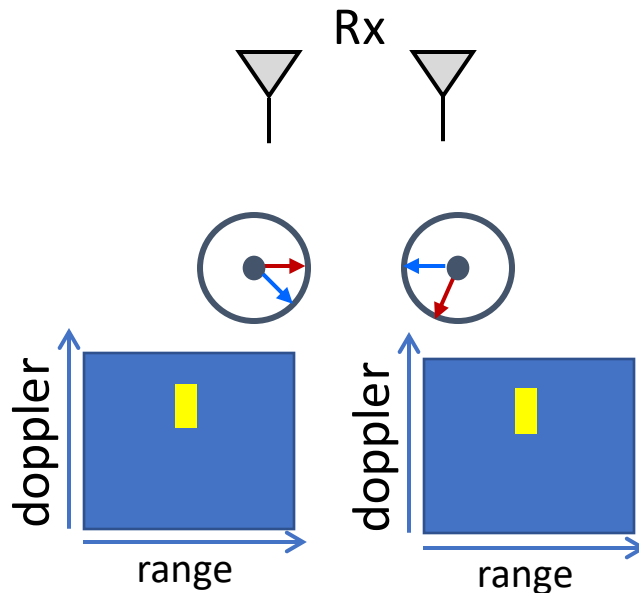
AoA Estimation
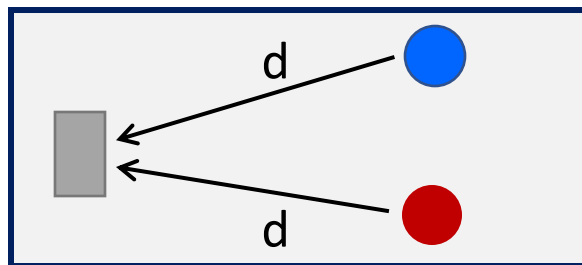
- An array of more receive antennas is needed
- <u>Angle-FFT</u>: FFT on the sequence of phasors corresponding to the Range-Doppler 2D-FFT peaks
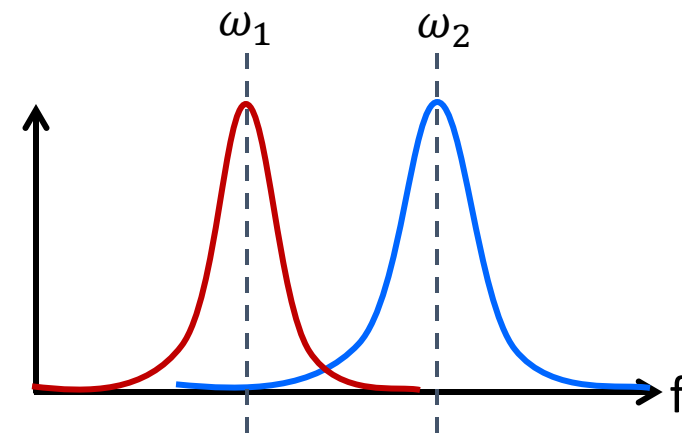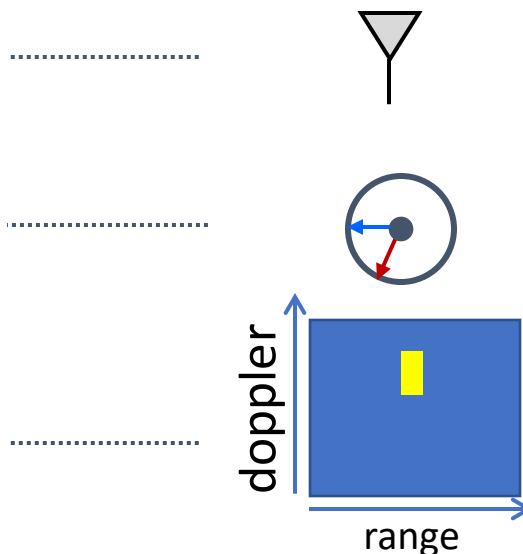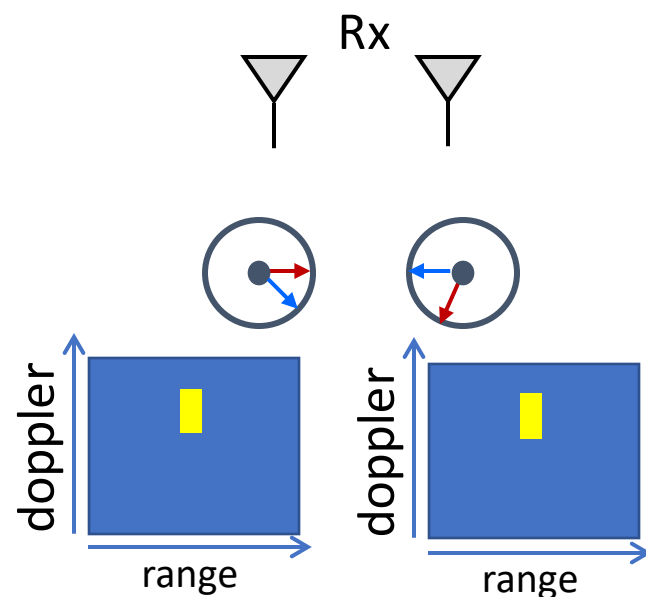
$$\theta_1 = \sin^{-1}(\frac{\lambda\omega_1}{2\pi s}), \theta_2 = \sin^{-1}(\frac{\lambda\omega_2}{2\pi s})$$

Angle Resolution

- θ_{res}: The minimum angle separation that can be differentiated by Angle-FFT.
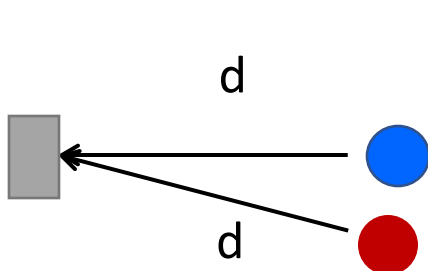
$$\Delta\omega = \frac{2\pi s}{\lambda}\left(\sin(\theta + \Delta\theta) - \sin(\theta)\right) \approx \frac{2\pi s}{\lambda \cos(\theta)\, \Delta\theta}$$

Recall FFT, $\Delta\omega > 2\pi/M$ ⬅ # of samples (antennas)

$$\rightarrow \Delta\theta > \frac{\lambda}{Ms\cos(\theta)}$$
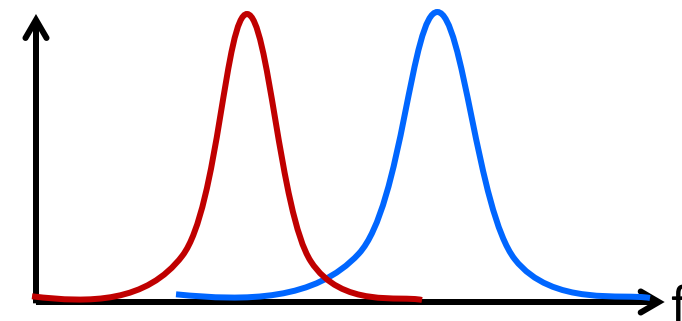
$$\theta_{res} = \frac{\lambda}{Ms\cos(\theta)}$$

Assume $s = \lambda/2, \theta = 0$

$$\theta_{res} = \frac{2}{M}$$

Ms: Aperture

Angle Resolution

- AoA resolution decreases as AoA increases.

$$\theta_{res} = \frac{\lambda}{Ms\cos(\theta)}$$

Resolution depends on θ. Best at $\theta = 0$.
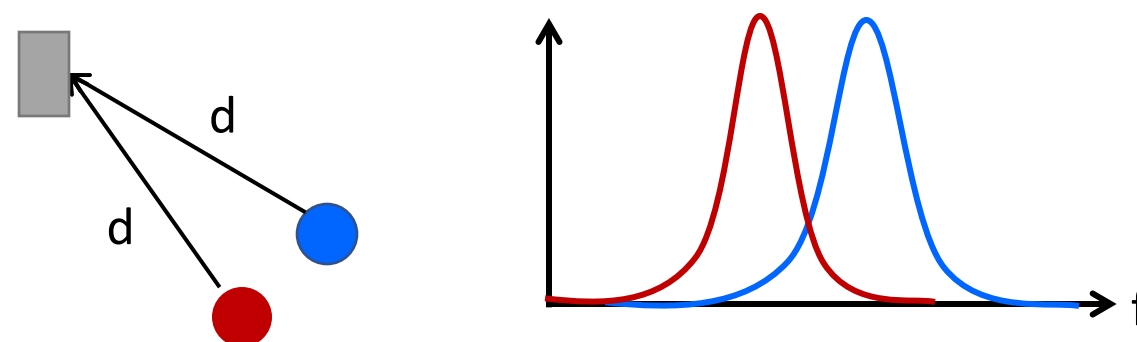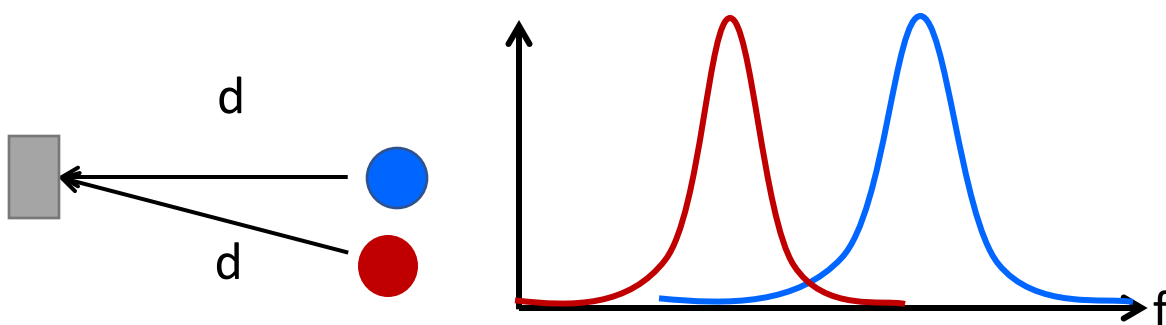
Beamforming

- ## Horn antenna
  - Mechanical motor

mmEye: Super-Resolution Millimeter Wave Imaging
Feng Zhang, Chenshu Wu, Beibei Wang, and K. J. Ray Liu
IEEE Internet of Things Journal, 2021.
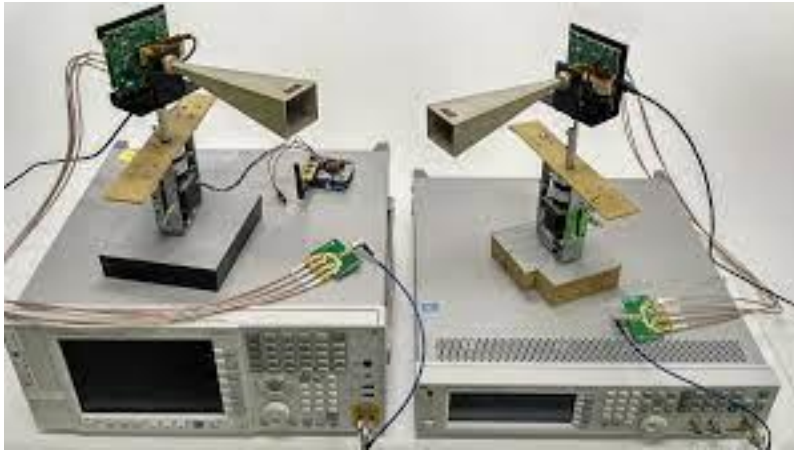
- ## Digital Beamforming
  - Classical beamforming
  - Minimum Variance Distortionless Response (MVDR) / Capon
  - MUSIC (MUltiple SIgnal Classification)

Image courtesy of DARPA

Radar Resolution
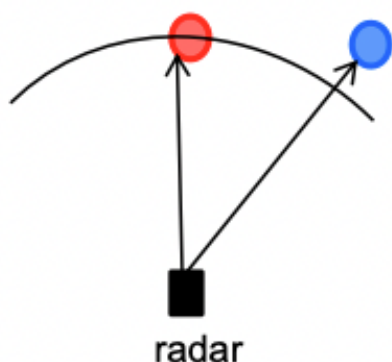
Angle
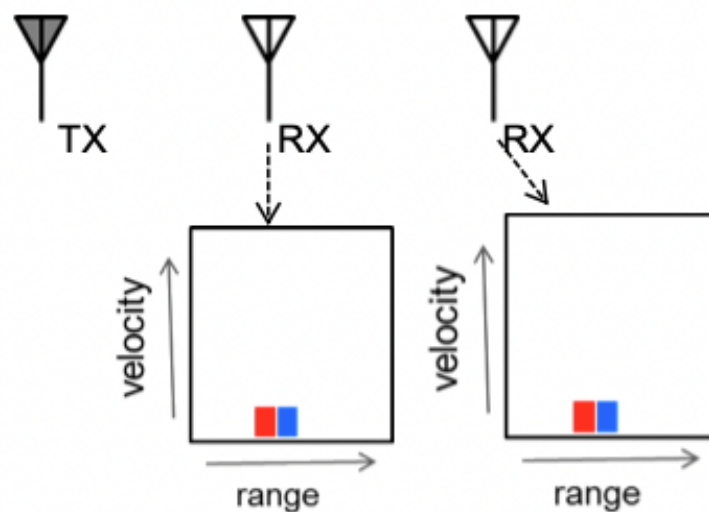
Range
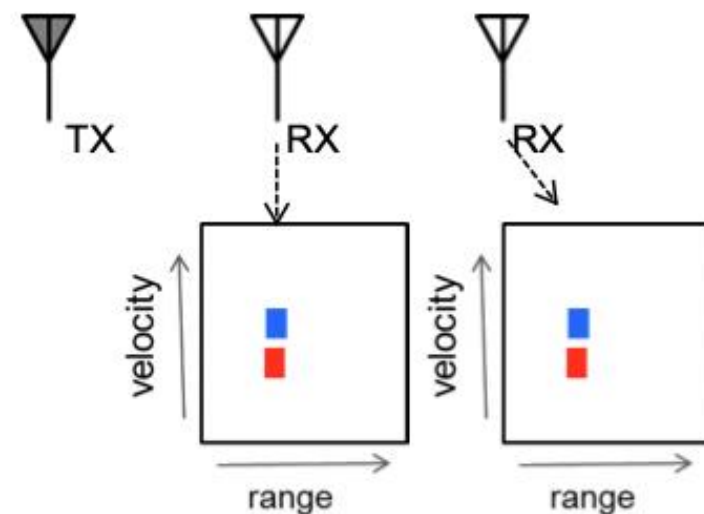
Doppler

Good range and velocity resolution can allow relatively poor angle/spatial resolution → Fewer antennas, smaller size.

Contents

- Basics of FMCW Radar Signals
- Range Estimation
- Doppler/Velocity Estimation
- Angle Estimation
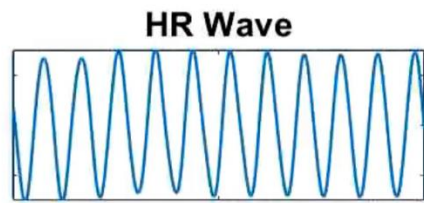- Periodicity Estimation
- FMCW Sensing Applications

Periodicity

- Measuring the frequency of <u>periodic movements</u>.
- Recall velocity estimation based on phase changes:

Tx chirp 1   Tx chirp 2
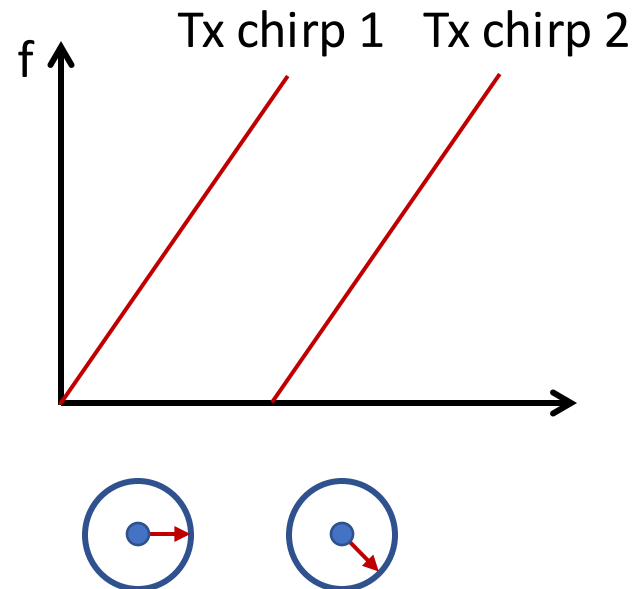
$$\Delta\phi = \frac{4\pi\Delta d}{\lambda} = \frac{4\pi v T_c}{\lambda}$$

What if the movement is periodic?

Periodicity – Vibration Object
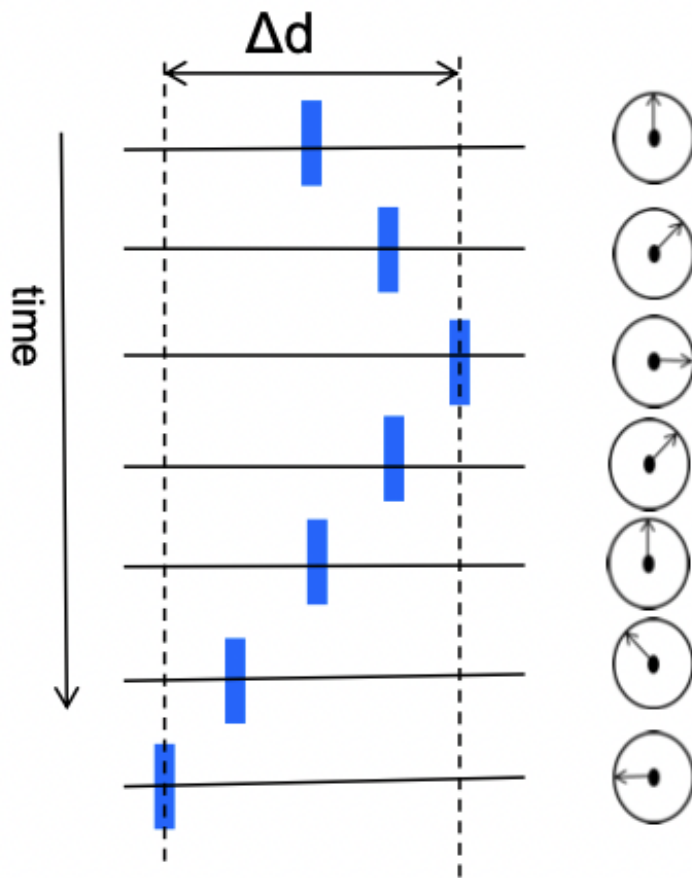
- Vibrating motor/machinery, heartbeat, breathing …

- Cause small but periodic changes in IF signal phase
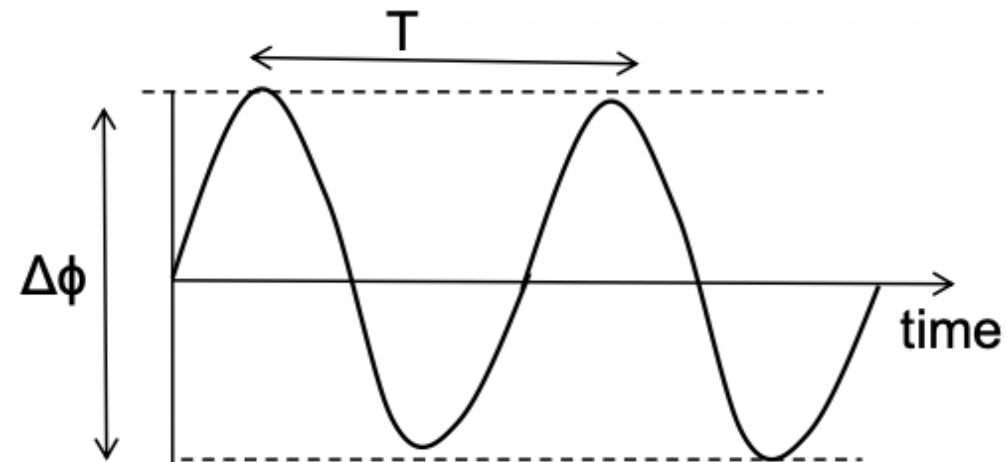
$$\omega = \frac{4\pi\Delta d}{\lambda}$$

Both amplitude and periodicity (frequency)

Contents

- Basics of FMCW Radar Signals

- Range Estimation

- Doppler/Velocity Estimation

- Angle Estimation

- Periodicity Estimation

- <u>FMCW Sensing Applications</u>

Imaging

mmEye: Super-Resolution Millimeter Wave Imaging, IEEE IoTJ, 2021
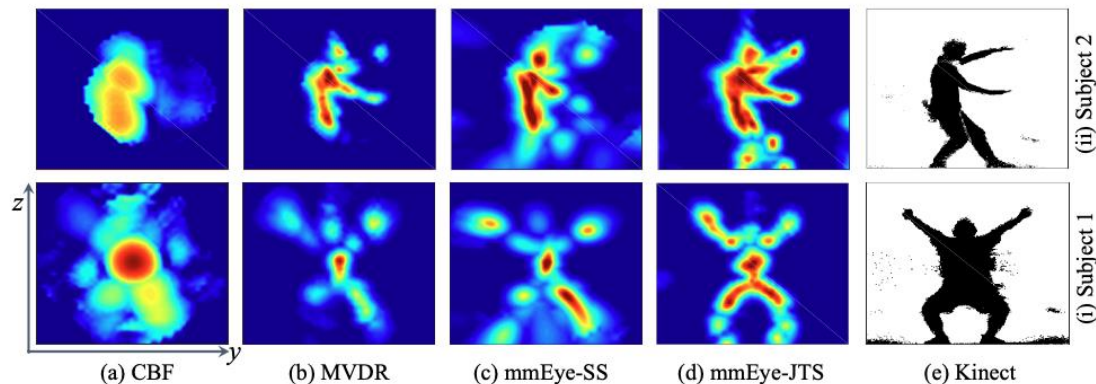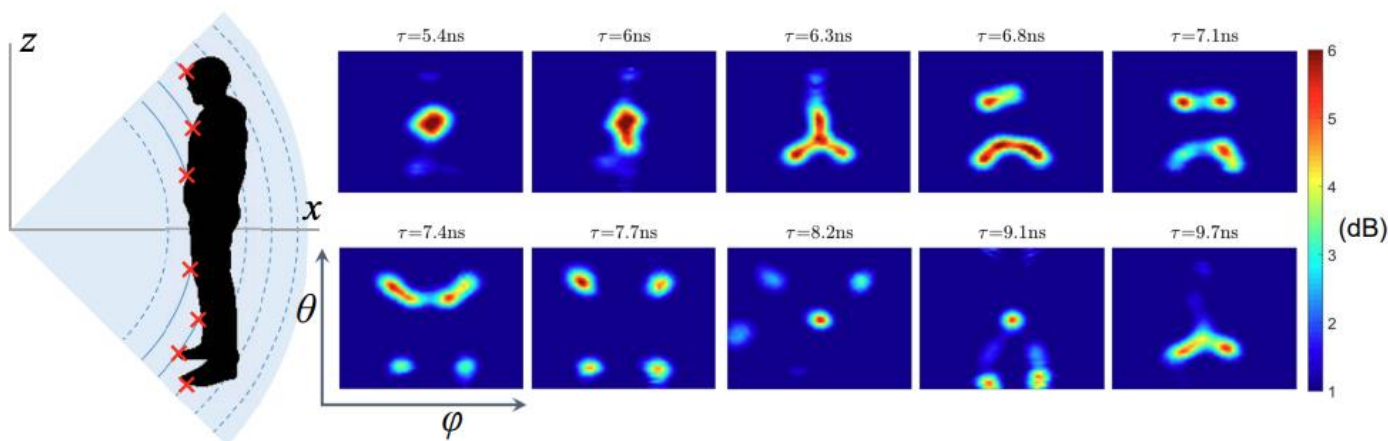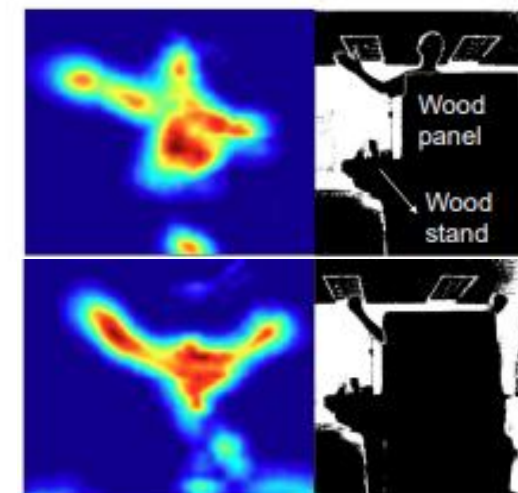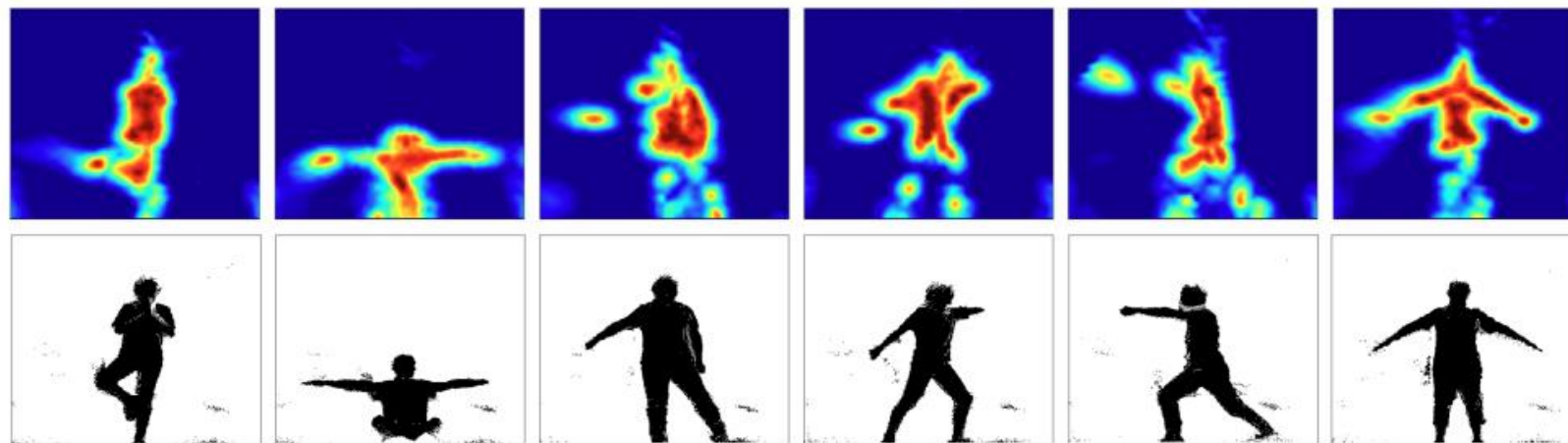
Vital Sign Monitoring

RR Wave
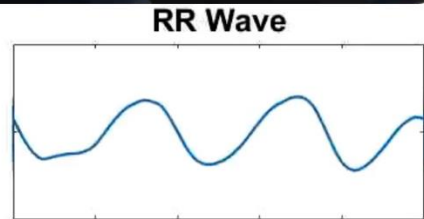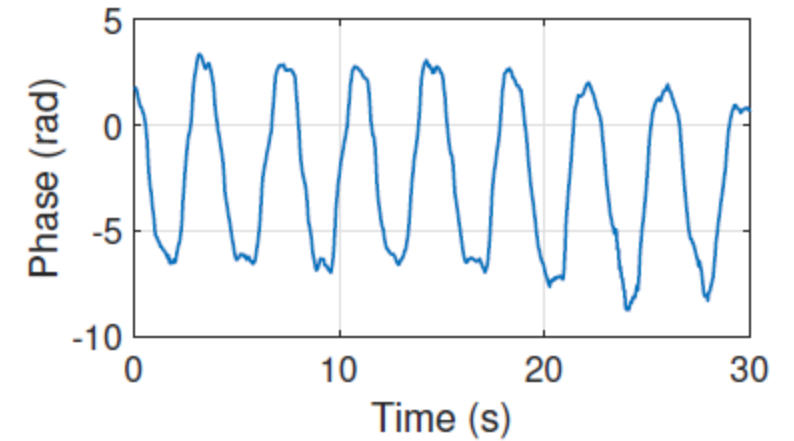
Respiration Rate Truth
16 rpm

Respiration Rate Estimation
16.06 rpm

HR Wave

Heart Rate Truth
66bpm

Heart Rate Estimation
66bpm

TI IWR1843

Driver Vital Signs Monitoring using Millimeter Wave Radio, IEEE IoTJ, 2022
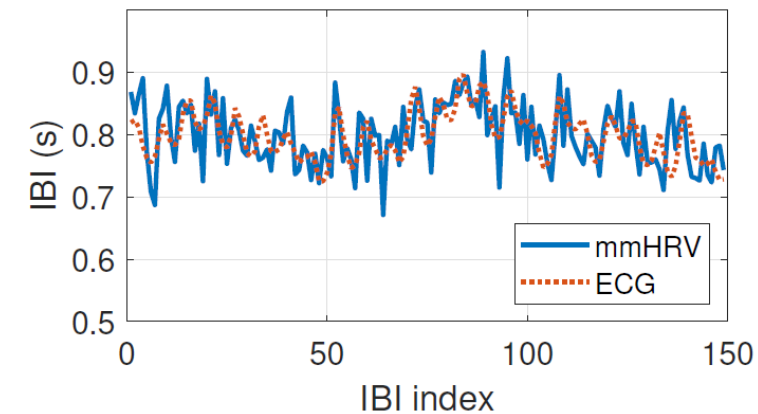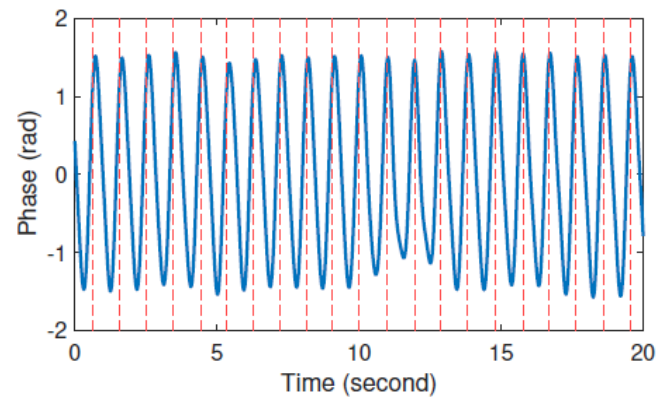
Gesture/Virtual Keyboard
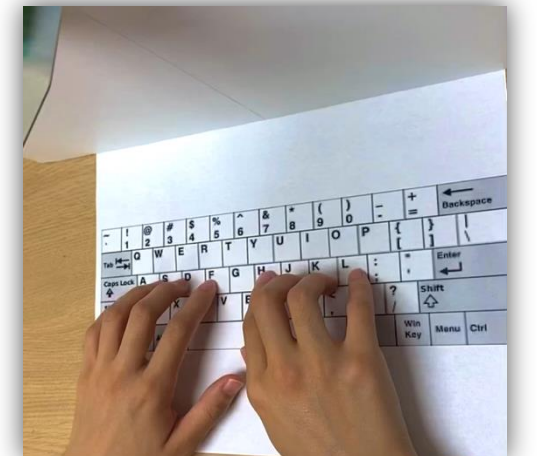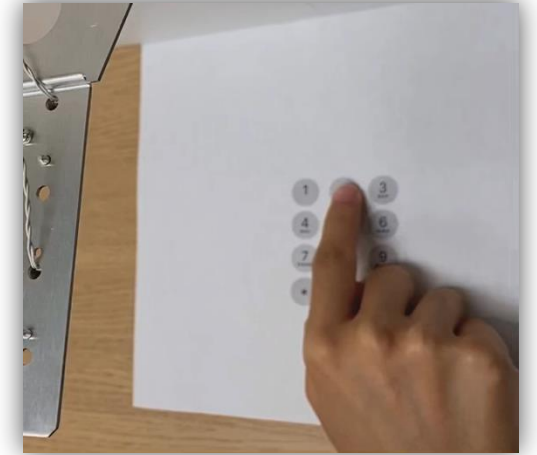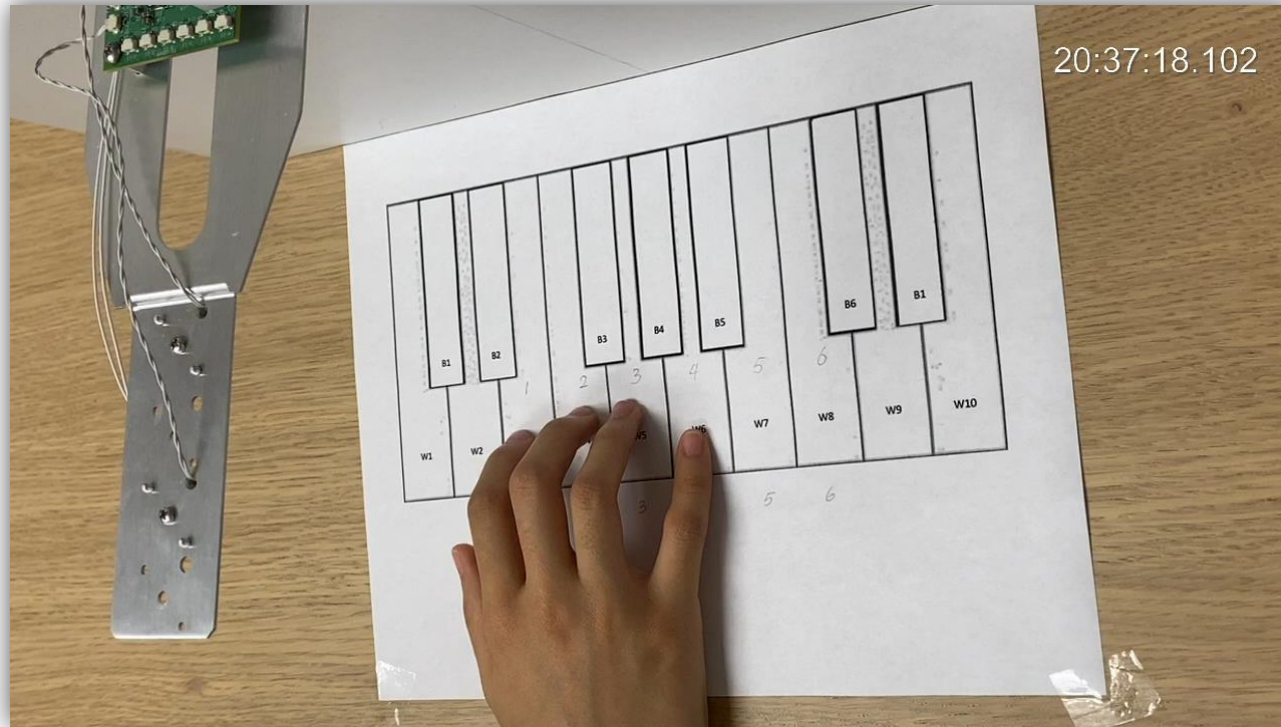
Ground truth: *w3 w3 w7 w7 w8 w8 w7 w6 w6 w5 w5 w4 w4 w3*

Estimation: *w3 w3 w7 w7 w8 w8 w7 w6 w6 w5 w5 w4 w4 w3*

Estimation = Ground truth

Gesture/Virtual Keyboard
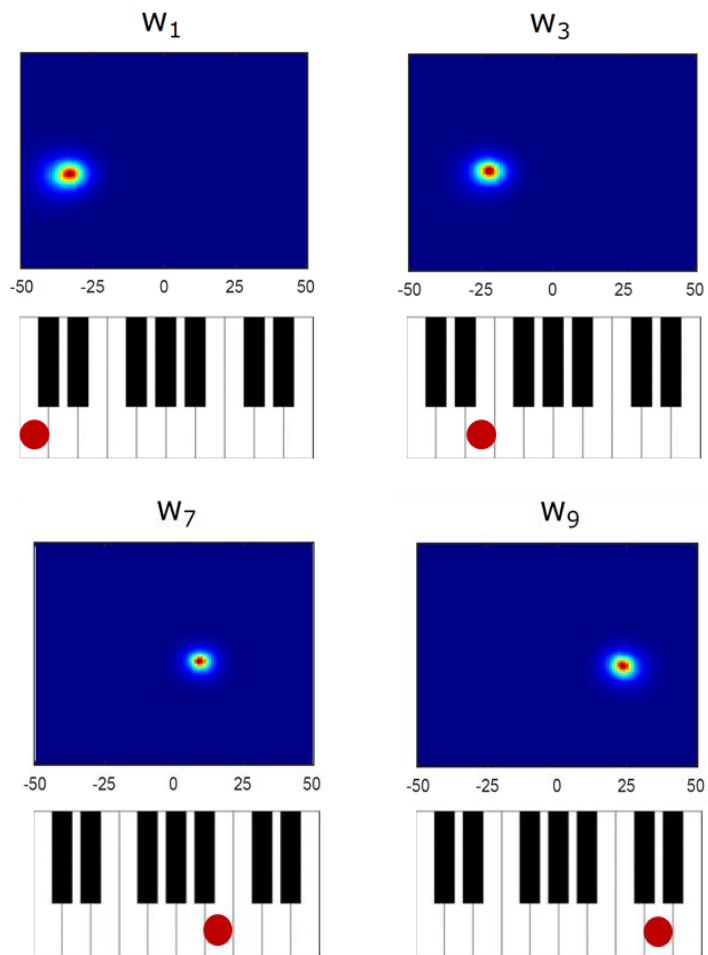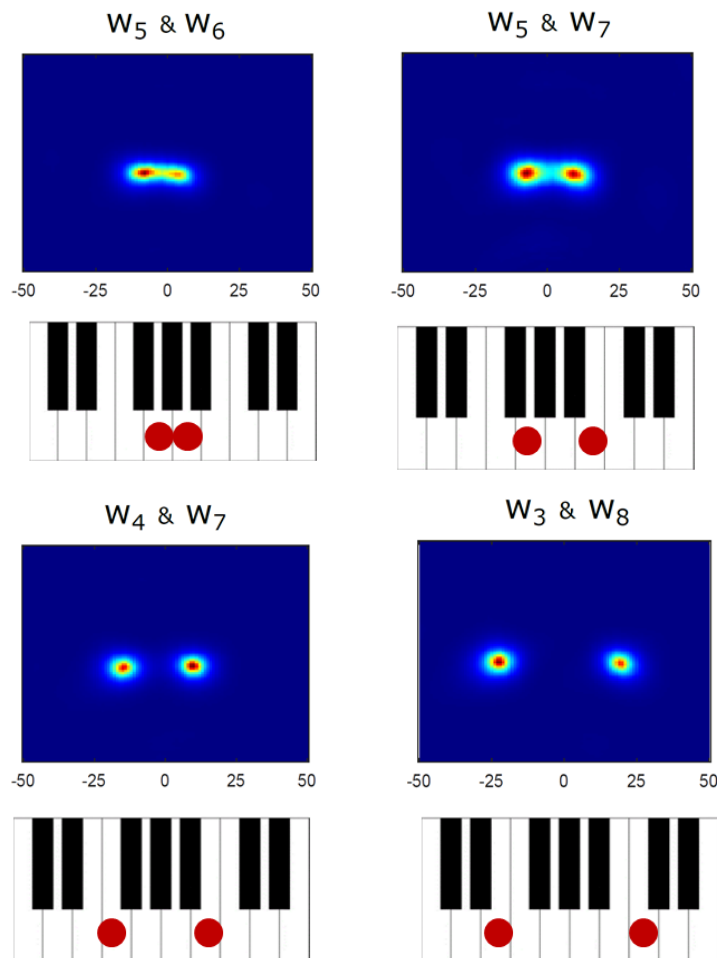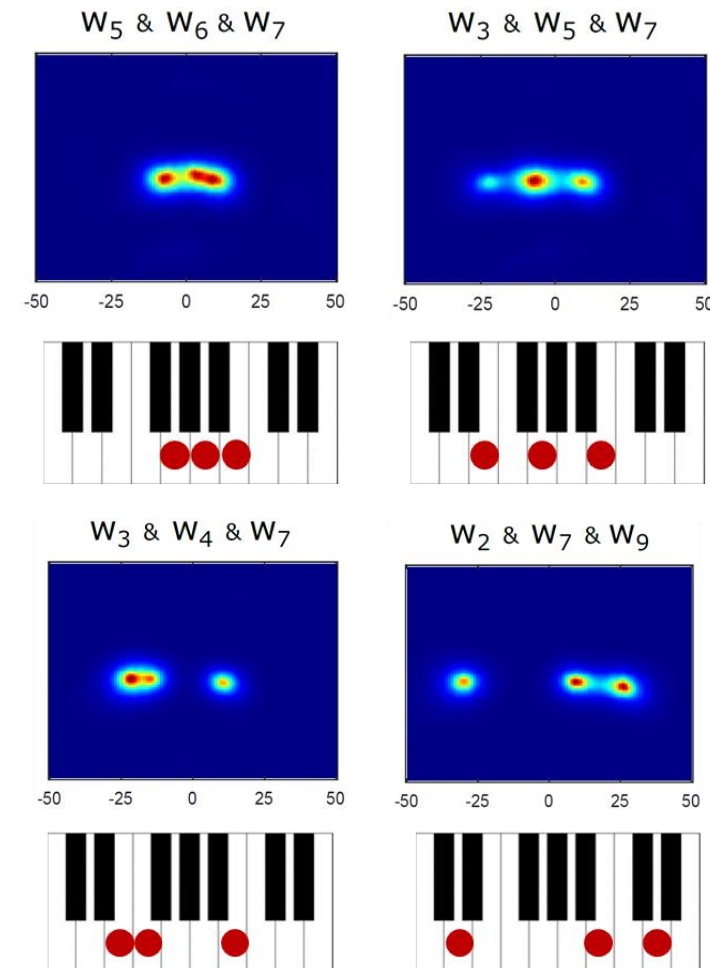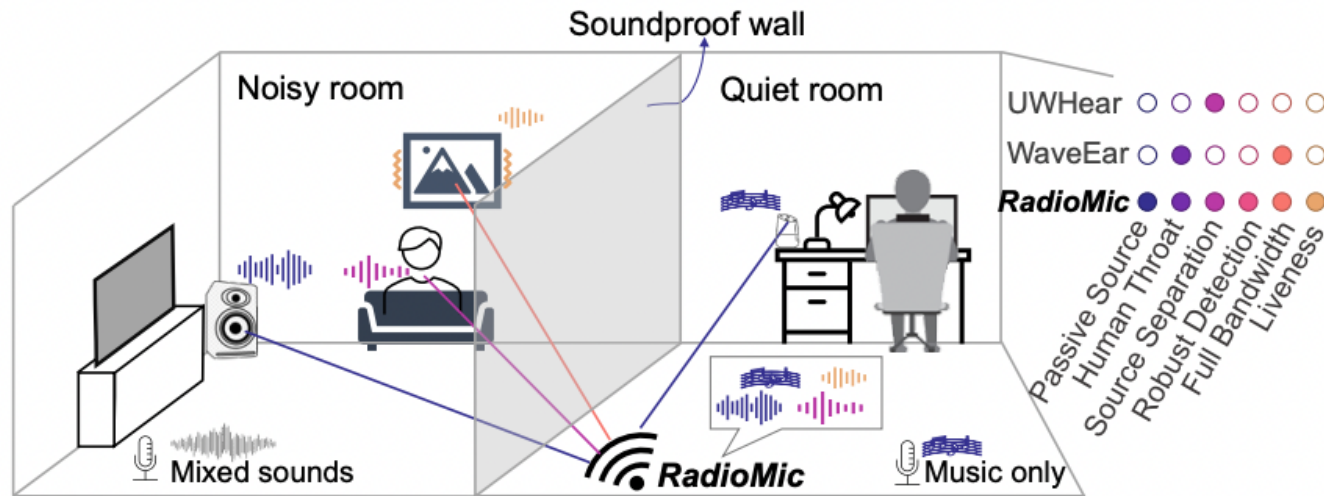

Y. Hu, B. Wang, C. Wu and K. J. R. Liu, mmKey: Universal Virtual Keyboard using A Single Millimeter Wave Radio, *IEEE IOTJ, 2021.*

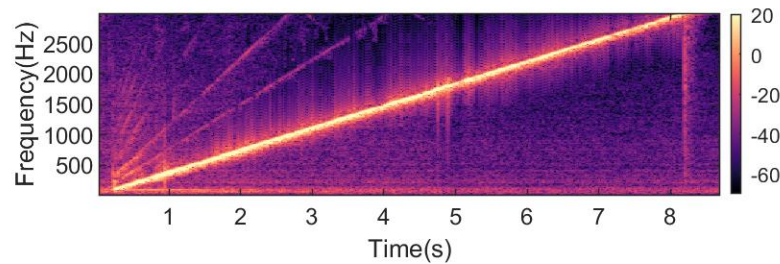# Sound Recovery from mmWave Sensing
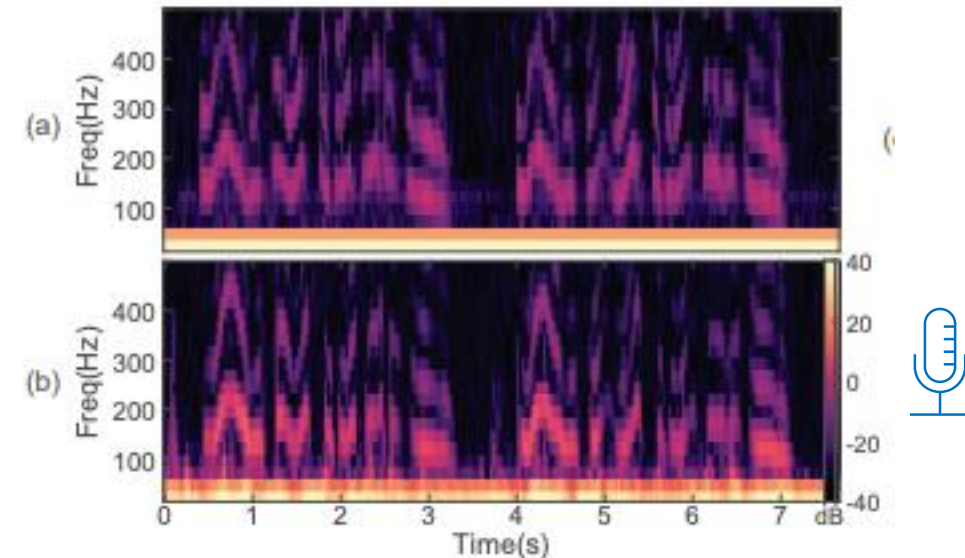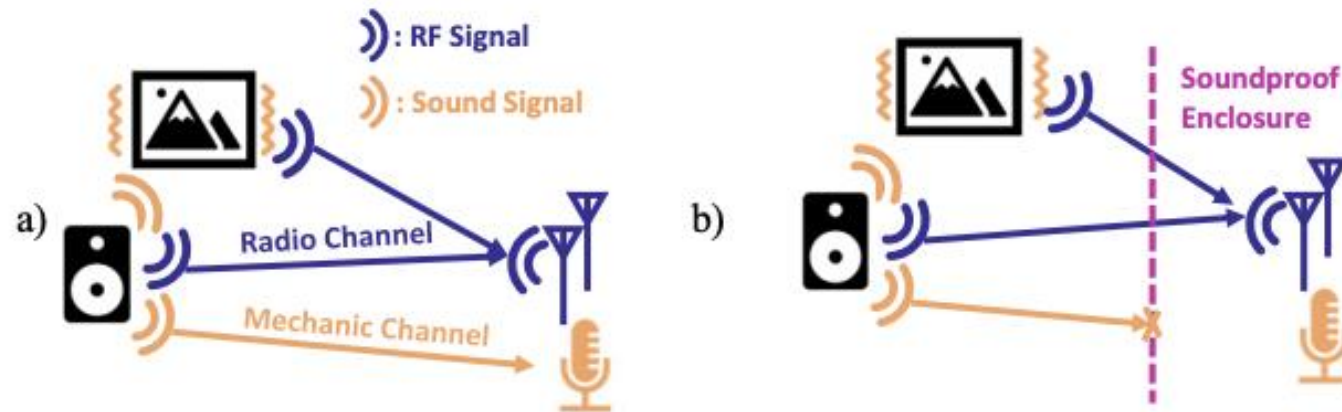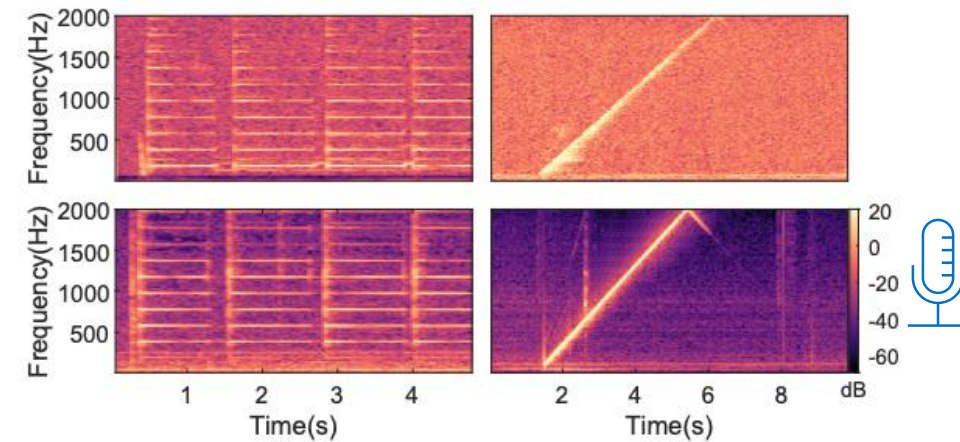
Ozturk, M. Z., Wu, C., Wang, B., & Liu, K. J. (2021). RadioMic: Sound sensing via mmWave signals. *IEEE IOTJ, 2022*.
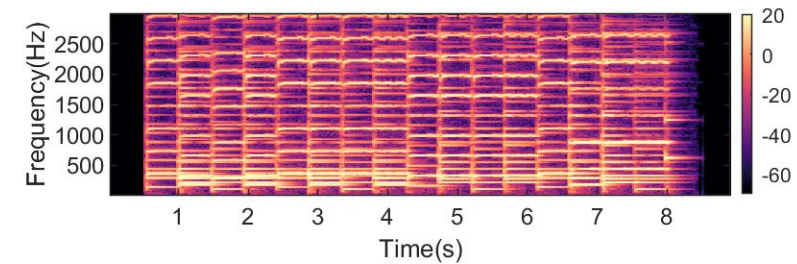
RadioMic: Examples

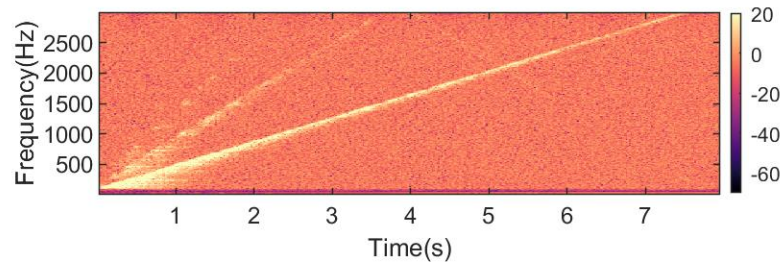**Frequency Sweep**

Music

Audio
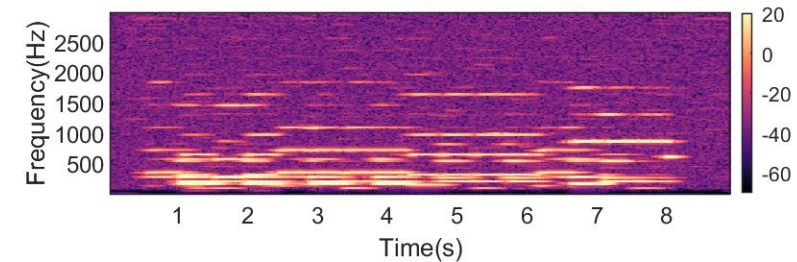
Radio

Fig 1. Frequency sweep

Fig 2. Instrumental music

Warning: Frequency sweep may be annoying to listeners
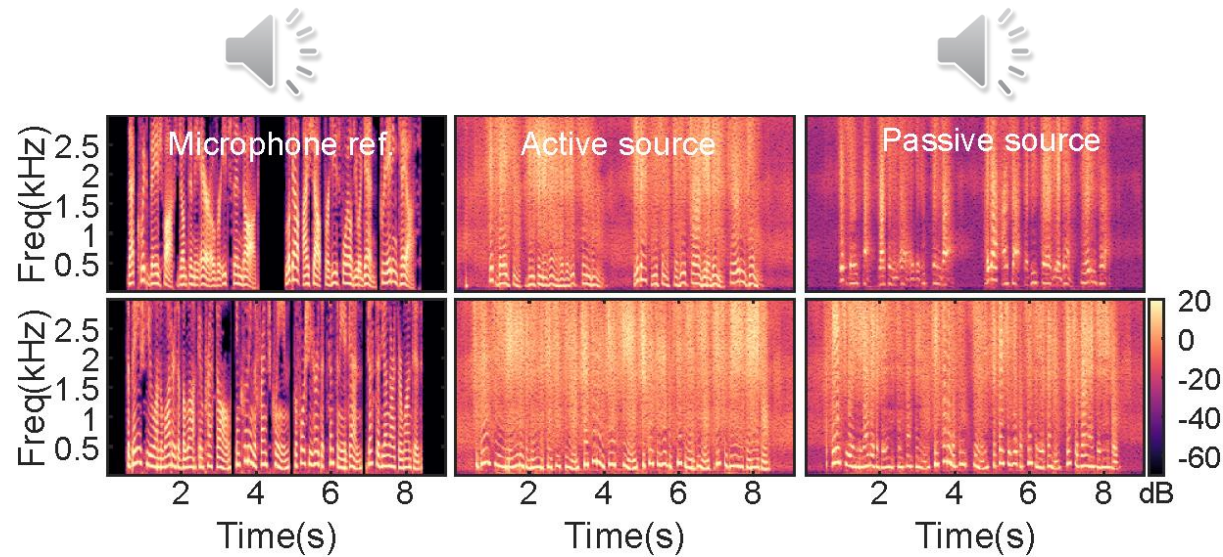
RadioMic: Examples
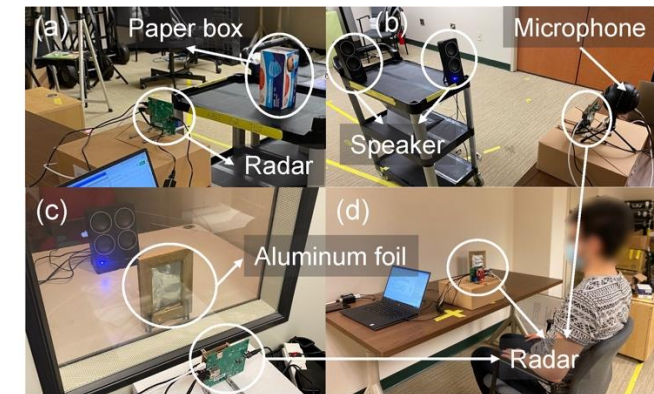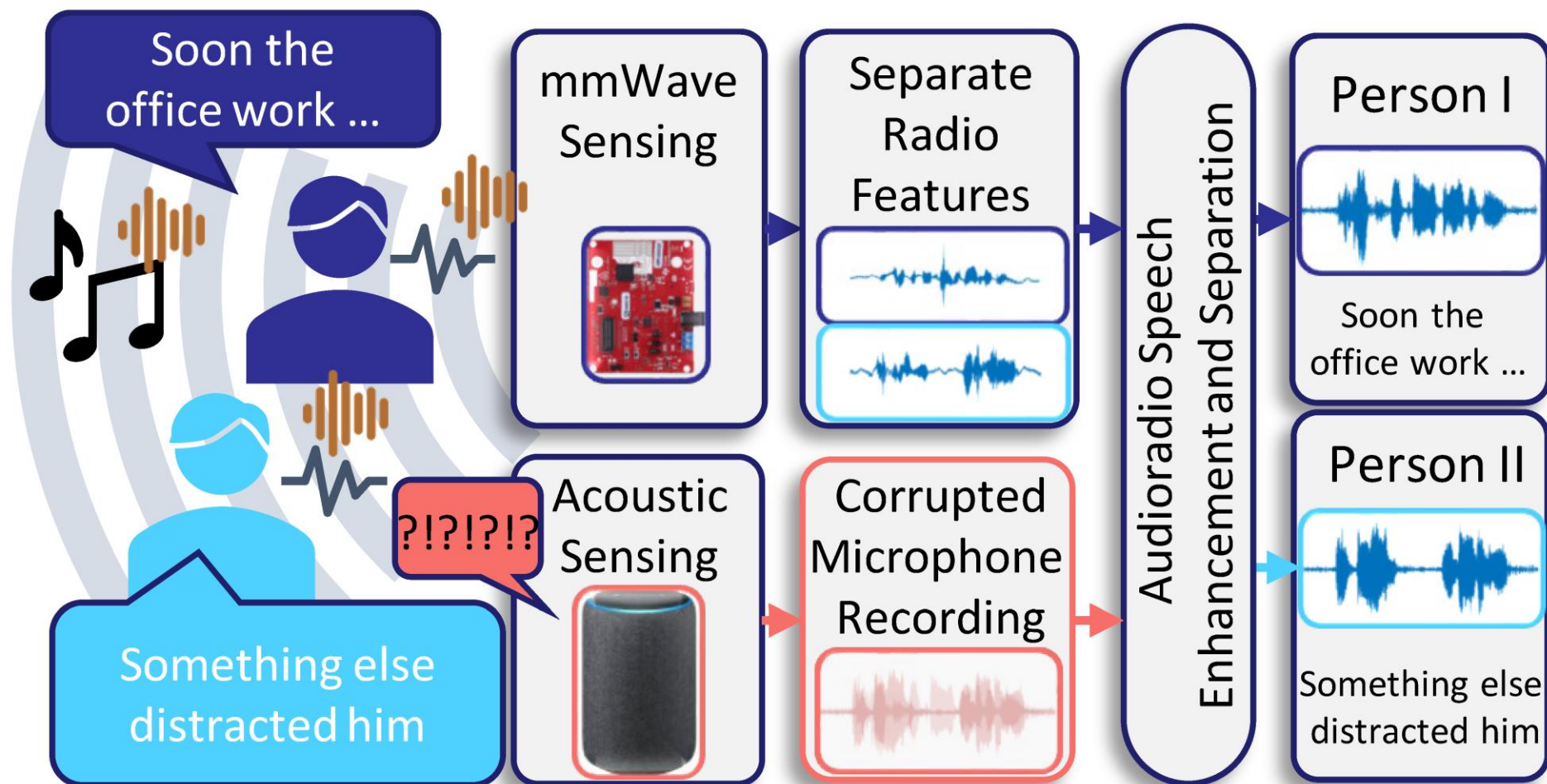

Fig 1. Example spectrograms with RadioMic

Fig 2. Data collection setups with RadioMic

That quick beige fox jumped in the air over each thin dog. Look out, I shout, for he's foiled you again, creating chaos

RadioSES: Speech Enhancement and Separation

Ozturk, M. Z., Wu, C., Wang, B., Wu, M., & Liu, K. J. (2022). RadioSES: mmWave-Based Audioradio Speech Enhancement and Separation System. IEEE/ACM TASLP, 2023.
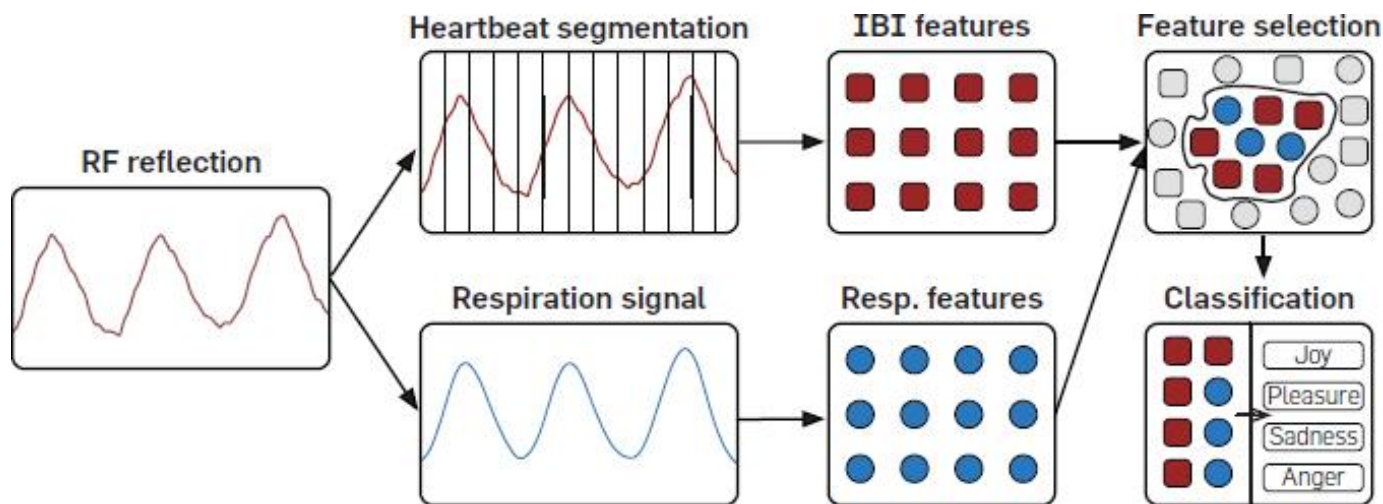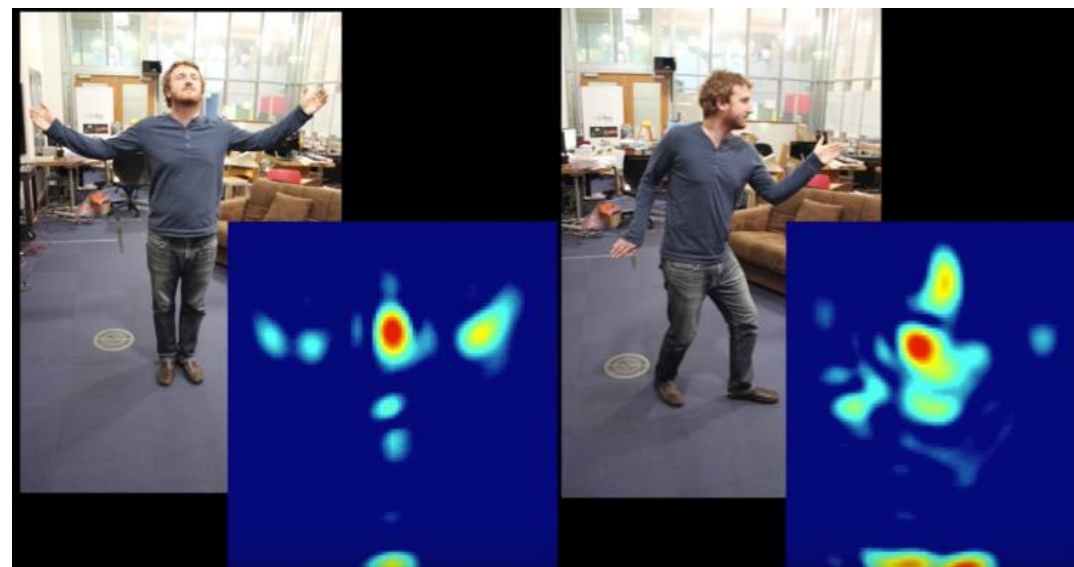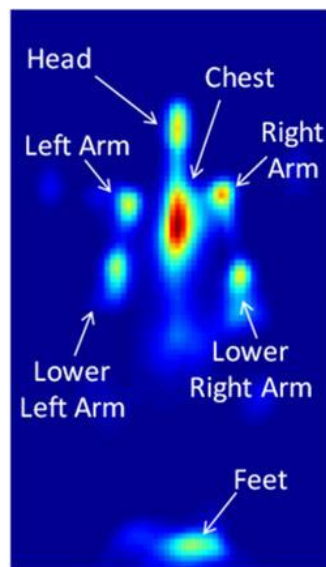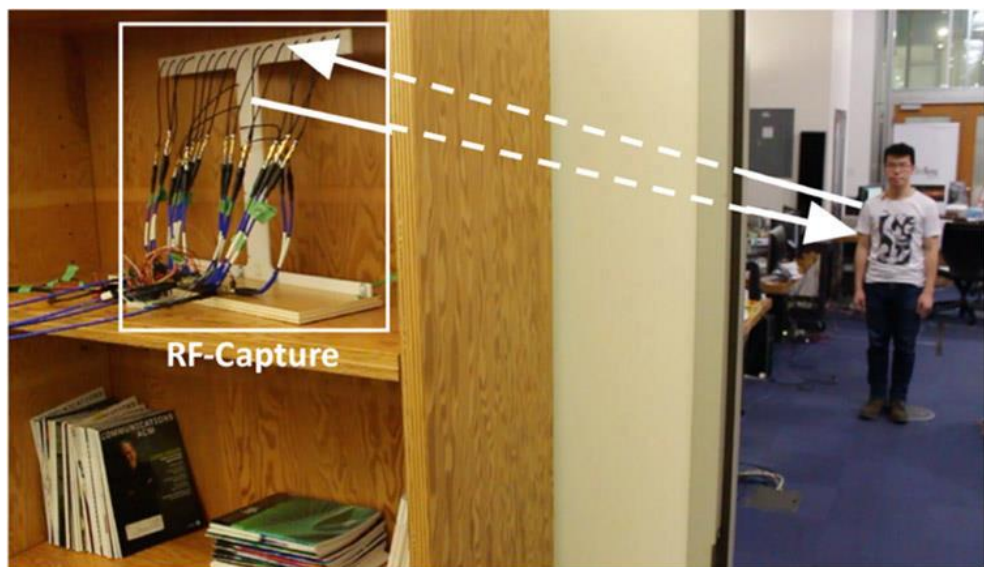
RadioSES: Audioradio approach

Ozturk, M. Z., Wu, C., Wang, B., Wu, M., & Liu, K. J. (2022). RadioSES: mmWave-Based Audioradio Speech Enhancement and Separation System. IEEE/ACM TASLP, 2023.

FMCW Radar on WiFi Frequency

A line of awesome work by Dina Katabi's team@MIT

Questions?

- Thank you!

- Next: Can we transform ubiquitous WiFi into a "Radar"?